Dror Bar-Natan: Talks: UCLA-191101 Everything around  $sl_{2+}^{\epsilon}$  is **DoPeGDO**. So what?

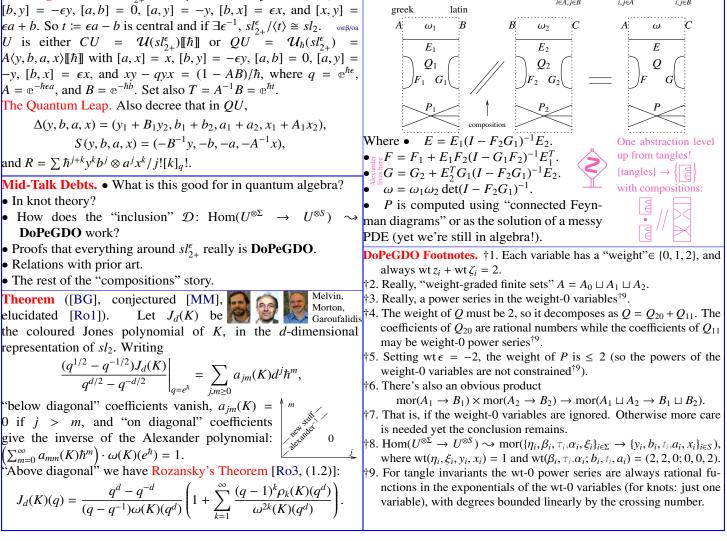
Thanks for inviting me to UCLA! Continues Rozansky [Ro1, 
 ωεβ:=http://drorbn.net/la19/
 Ro2, Ro3] and Overbay [Ov], joint with van der Veen [BV].



Abstract. I'll explain what "everything around" means: classical Knot theorists should rejoice because all this leads to very poand quantum m,  $\Delta$ , S, tr, R, C, and  $\theta$ , as well as P,  $\Phi$ , J,  $\mathbb{D}$ , werful and well-behaved poly-time-computable knot invariants. and more, and all of their compositions. What **DoPeGDO** means: Quantum algebraists should rejoice because it's a realistic playthe category of Docile Perturbed Gaussian Differential Operators. ground for testing complicated equations and theories. And what  $sl_{2+}^{\epsilon}$  means: a solvable approximation of the semisimple Lie algebra  $sl_2$ .

**Conventions.** 1. For a set *A*, let 
$$z_A := \{z_i\}_{i \in A}$$
 and let  $\zeta_A := \{z_i^* = \zeta_i\}_{i \in A}$ .<sup>†1</sup> 2. Everything converges!

Less Abstract **DoPeGDO** := The category with objects finite sets<sup> $\dagger 2$ </sup> and mor( $A \rightarrow B$ ):  $\{\mathcal{F} = \omega \exp(Q + P)\} \subset \mathbb{Q}[[\zeta_A, z_B, \epsilon]]$  $\mathcal{D}_{\rightarrow}$  $S: U \rightarrow U$ Where: •  $\omega$  is a scalar.<sup>†3</sup> • Q is a "small"  $\epsilon$ -free  $m: U \otimes U \rightarrow U$  $\Delta: U \rightarrow U \otimes U$ quadratic in  $\zeta_A \cup z_B$ .<sup>†4</sup> • *P* is a "docile perturba-4D Metrized Lie Algebras tion":  $P = \sum_{k \ge 1} \epsilon^k P^{(k)}$ , where deg  $P^{(k)} \le 2k + 2$ .<sup>†5</sup> solvable • Compositions:<sup>†6</sup> cup cap algebras  $\mathcal{F}/\!\!/\mathcal{G} = \mathcal{G} \circ \mathcal{F} \coloneqq \left(\mathcal{G}|_{\zeta_i \to \partial_{z_i}} \mathcal{F}\right)_{z_i=0} = \left(\mathcal{F}|_{z_i \to \partial_{\zeta_i}} \mathcal{G}\right)_{z_i=0}$  $sl_{2}^{\epsilon}$  $\rightarrow U/wx = xw$  $R \in OU \otimes OU$  $C^{\pm 1} \in QU$ **Cool!**  $(V^*)^{\otimes \Sigma} \otimes V^{\otimes S}$  explodes; the ranks of qua-Cartan's  $\theta$ , the Abelian dratics and bounded-degree polynomials grow the Vassiliev algebra Dequantizator, slowly!<sup>†7</sup> Representation theory is over-rated! and more.. algebras isomorphic Cool! How often do you see a computational toto  $sl_{2+} \coloneqq sl_2 + 1D$  $\Phi \in CU^{\otimes}$  $J \in CU \otimes CU$ olbox so successful? **Our Algebras.** Let  $sl_{2+}^{\epsilon} \coloneqq L\langle y, b, a, x \rangle$  subject to [a, x] = x, **Compositions (1).** In mor $(A \to B)$ ,  $Q = \sum_{i \in A, j \in B} E_{ij} \zeta_i z_j + \frac{1}{2} \sum_{i, j \in A} F_{ij} \zeta_i \zeta_j + \frac{1}{2} \sum_{i, j \in B} G_{ij} z_i z_j$ 



Video and more: http://www.math.toronto.edu/~drorbn/Talks/CRM-1907, http://www.math.toronto.edu/~drorbn/Talks/UCLA-191101.