

# Is there math after calculus?



Written and created by Dr. Scherich

<https://www.youtube.com/watch?v=xgKc7dFz-ko>

# Video Interviews - Connections

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|                                                              |                                            |                                                         |
|--------------------------------------------------------------|--------------------------------------------|---------------------------------------------------------|
| Dr. Lauren Ancel Meyers<br>Biology, Statistics, Data Science | Dr. Lyla El-Fayomi<br>Neuroscience         | Nick Fellini<br>Mathematics                             |
| Dr. Anna Goldenberg<br>Machine Learning for Health           | Dr. Mjaye Mazwi<br>Pediatric Critical Care | Dr. Nicole Mideo<br>Ecology and Evolutionary<br>Biology |
| Rebecca Moranis<br>Music Theory                              | Dr. Abe Pressman<br>Biochemist             | Dr. Elizabeth Wong<br>Paediatric Pharmacist             |

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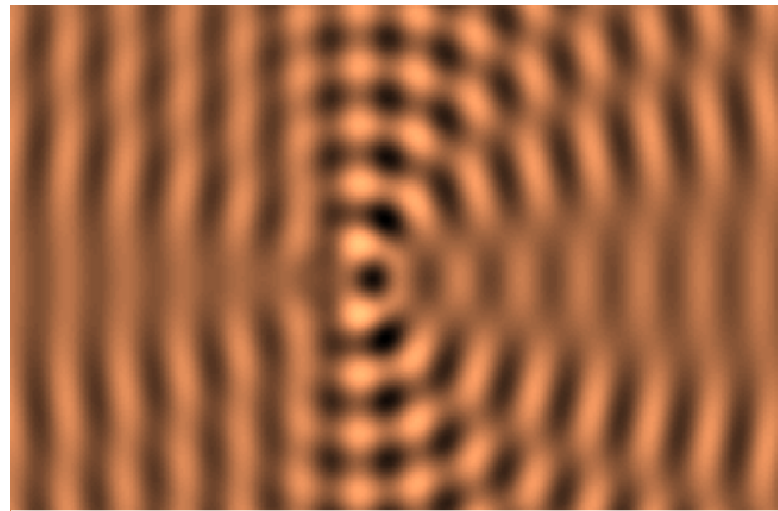
Quercus > Modules > Reading Week

Fall 2023

MAT135 Calculus 1

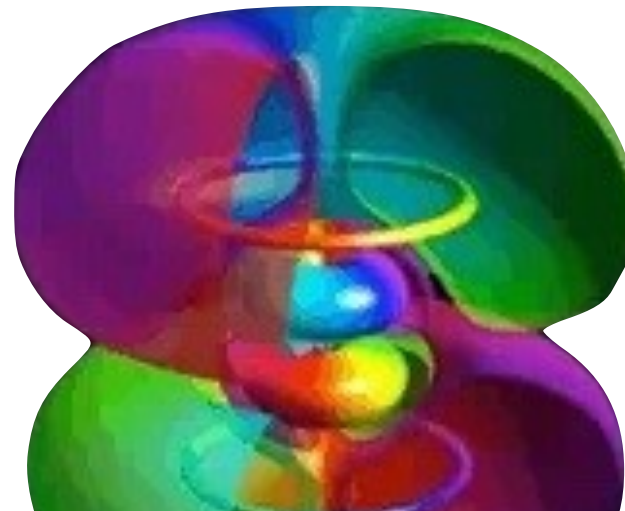


# Teaching Team



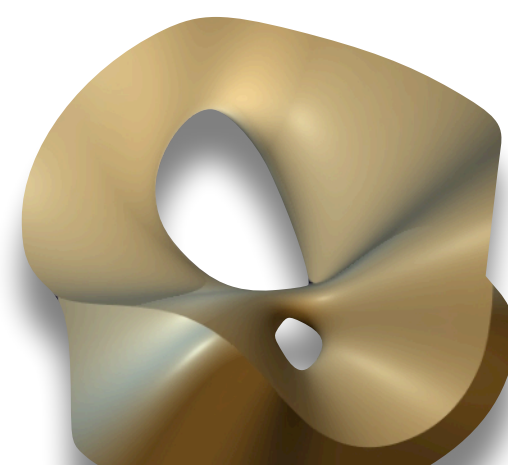
## Partial Differential Equations

Afiny Akdemir  
Sebastian Gherghe



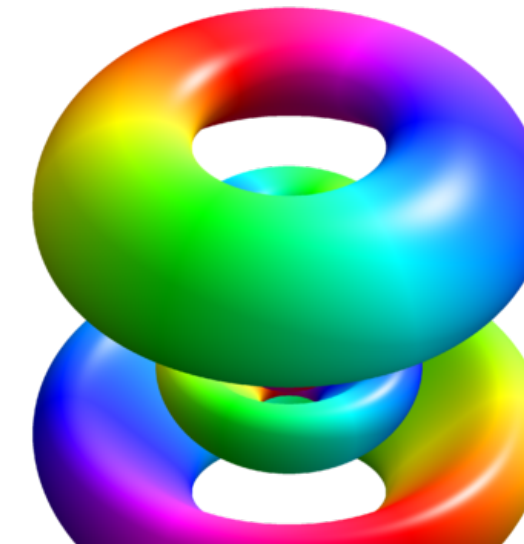
## Differential Geometry

Gavin Hurd



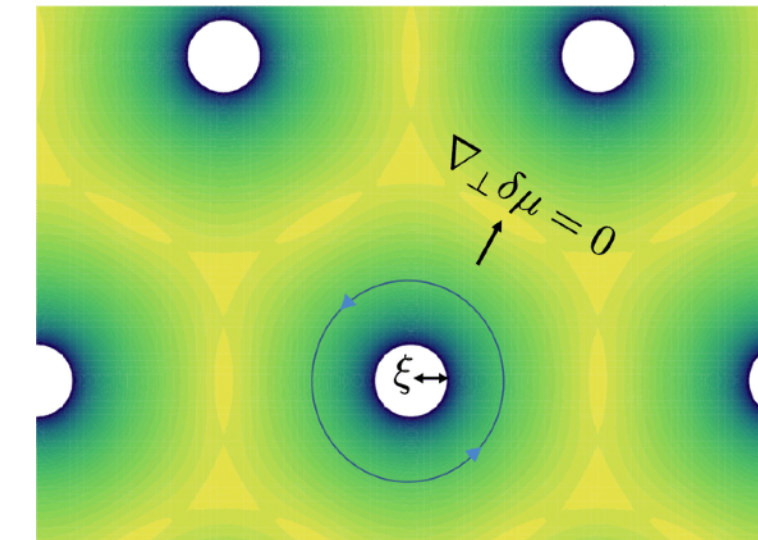
## Algebraic Geometry

Soheil Memarian  
Sorkhabi



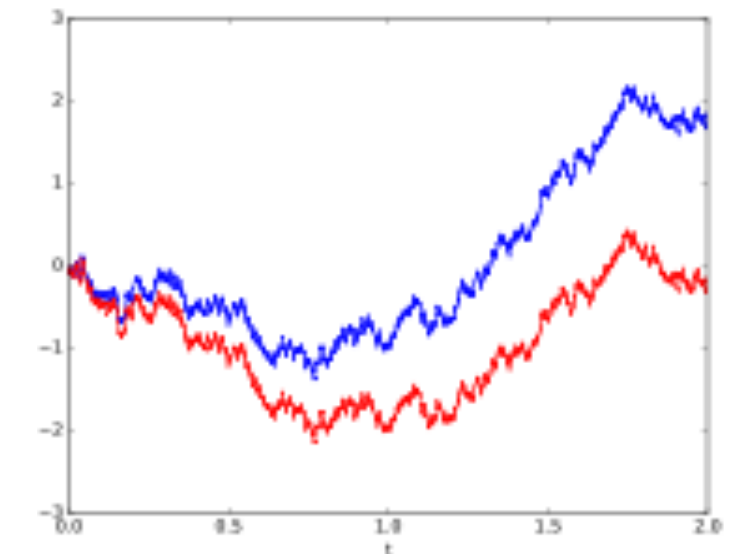
## Applied Probability

Dmitry Panchenko



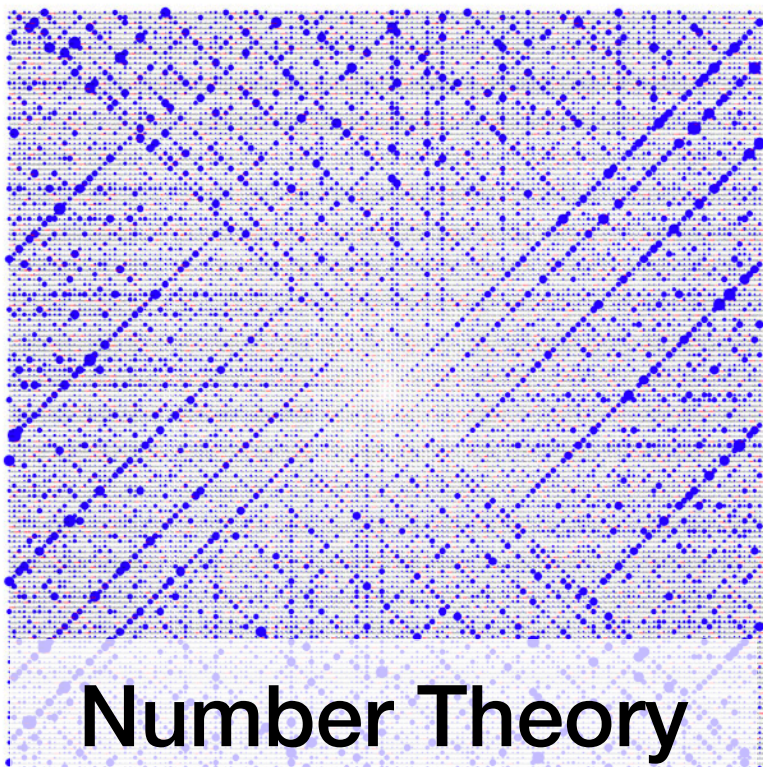
## Calculus of Variations

Bernardo Galvão-Sousa



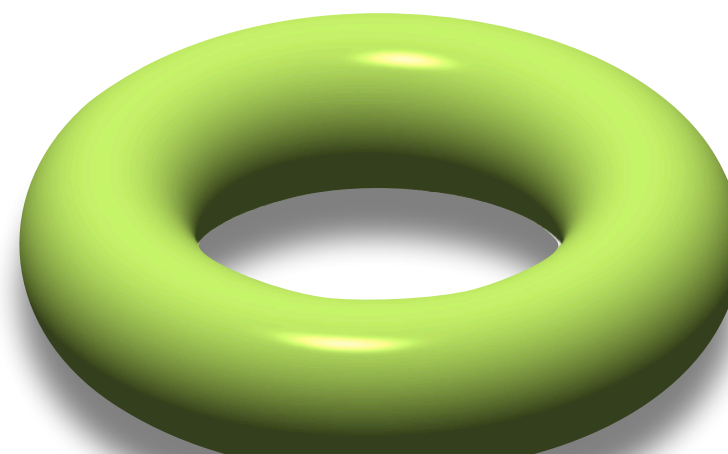
## Stochastics

Virginia Pedreira



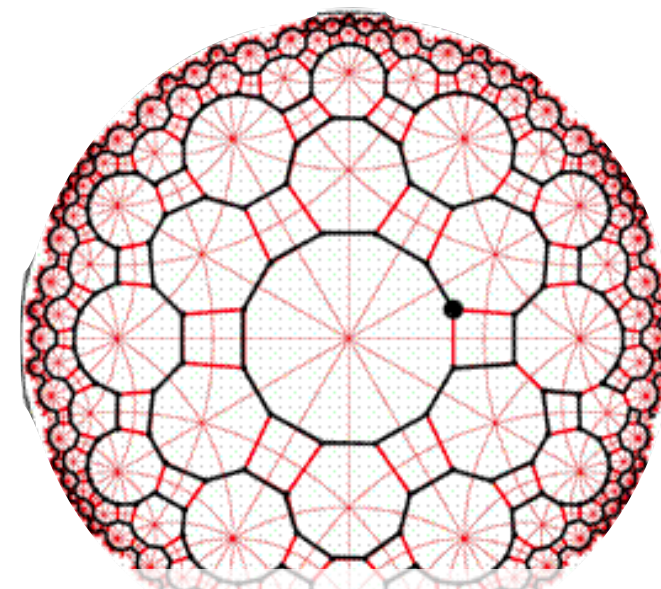
## Number Theory

Erik Holmes



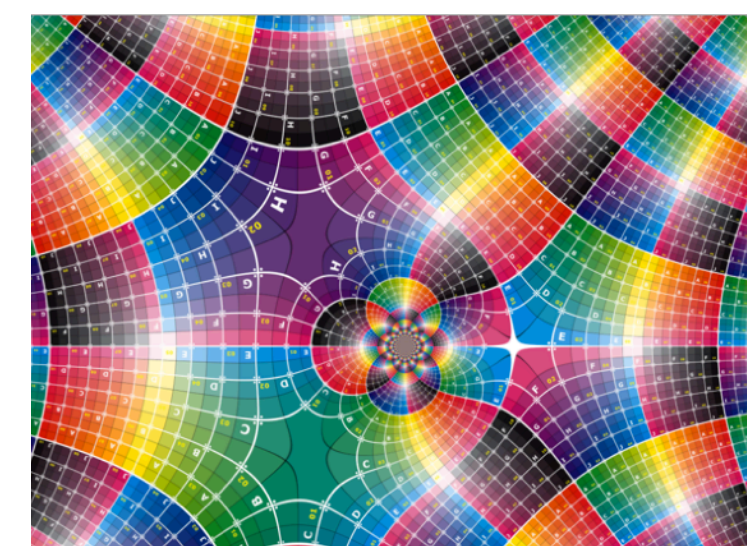
## Geometric Topology

Aleksandr Berdnikov  
Clovis Hamel



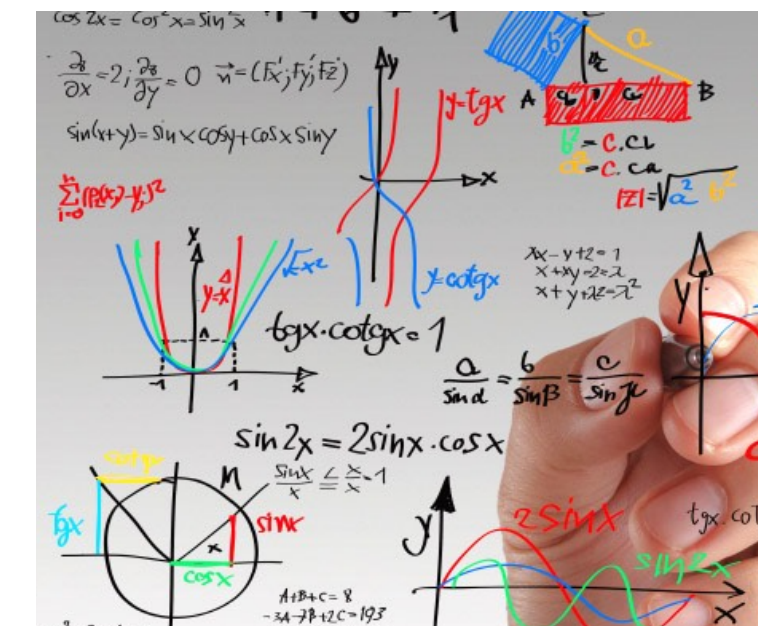
## Representation Theory

William Sokurski



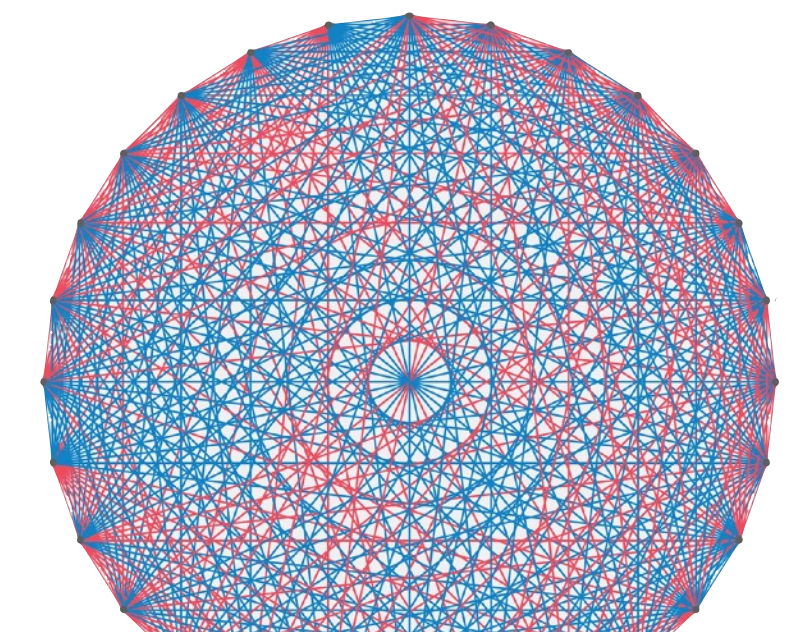
## Complex Function Theory

Emile LeBlanc



## Math Education

Bernardo Galvão-Sousa



## Ramsey Theory

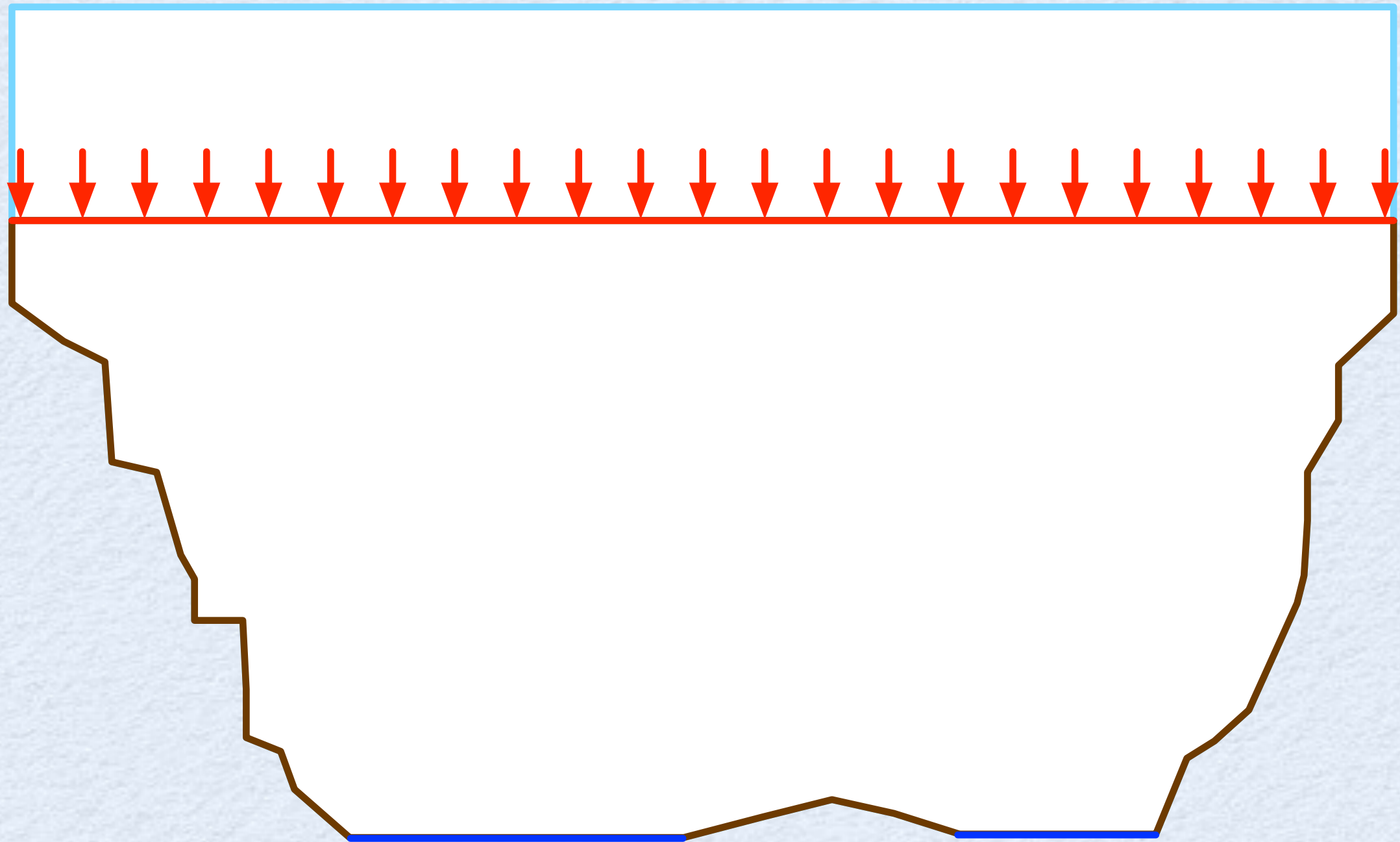
Jamal Kawach

Fall 2023

MAT135 Calculus 1



# structural optimization





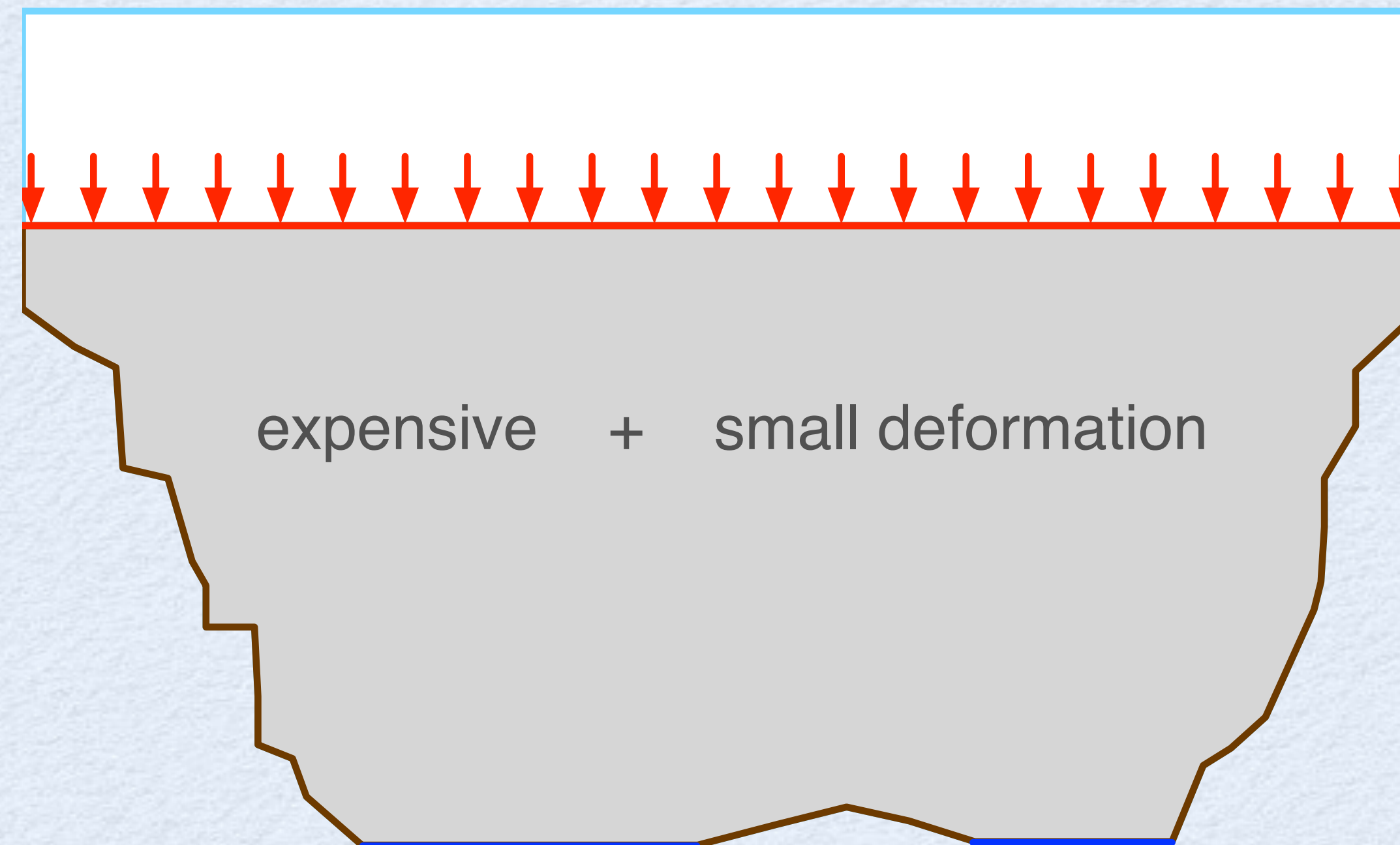
# structural optimization

minimize

cost of material + deformations



# structural optimization



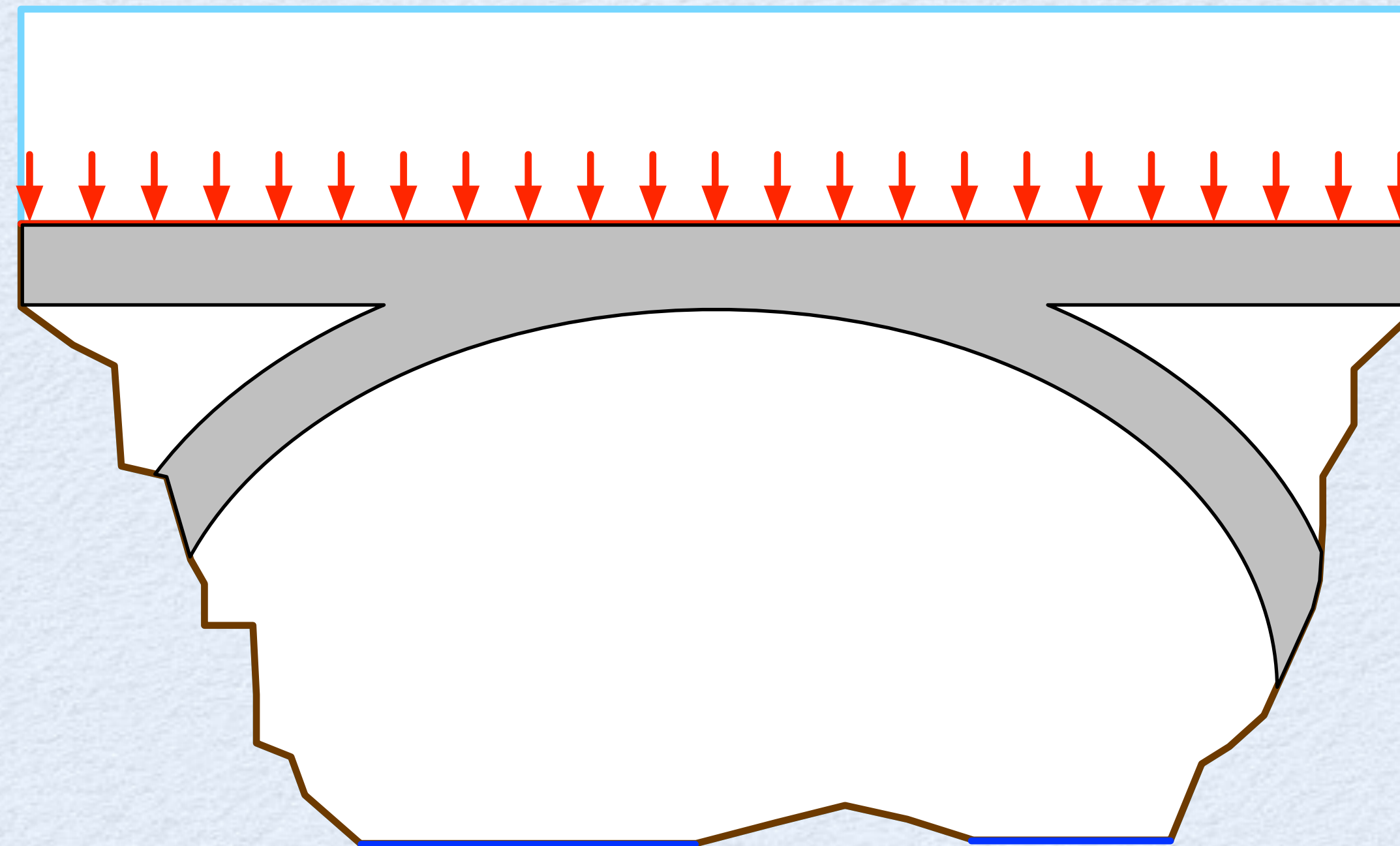


# structural optimization





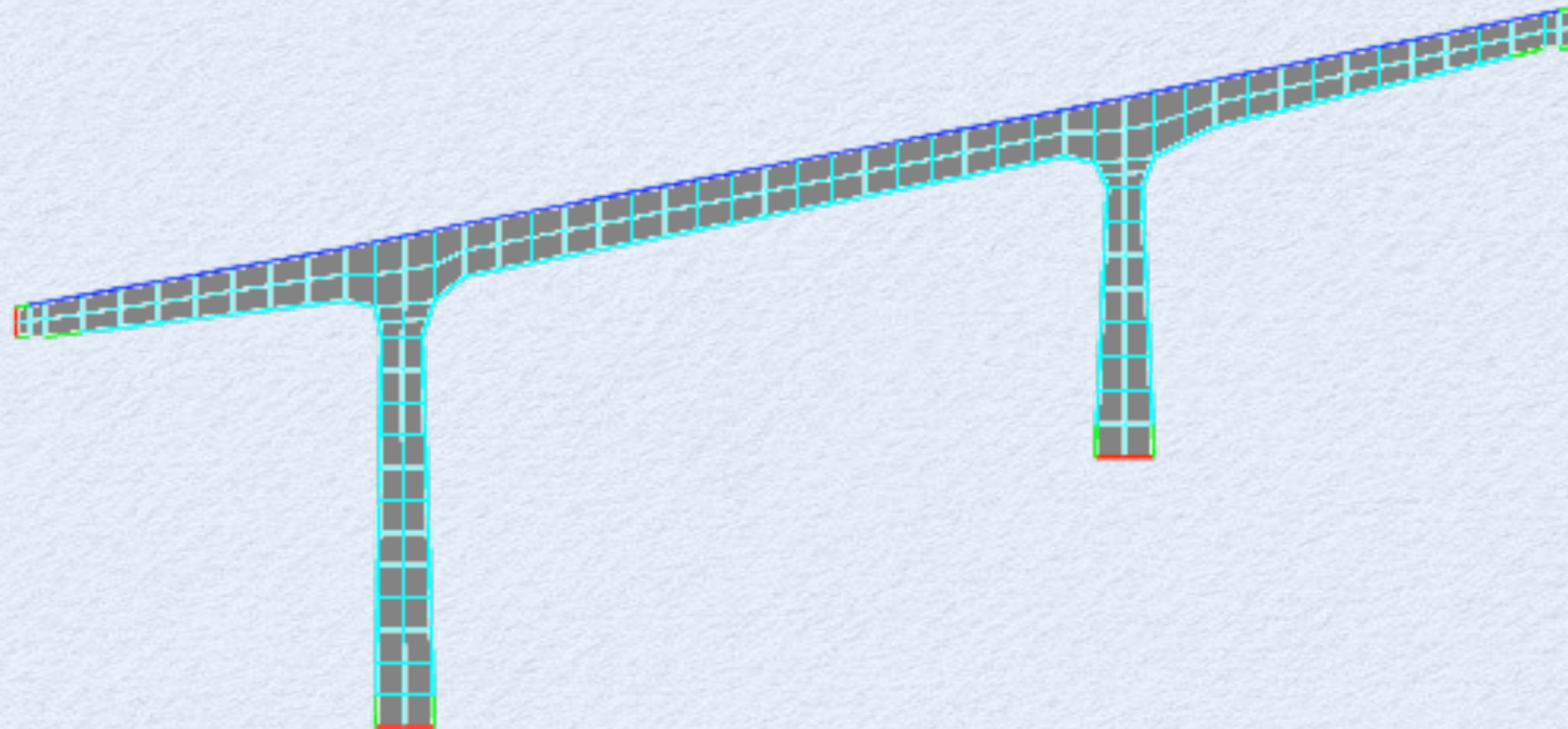
# structural optimization





# structural optimization

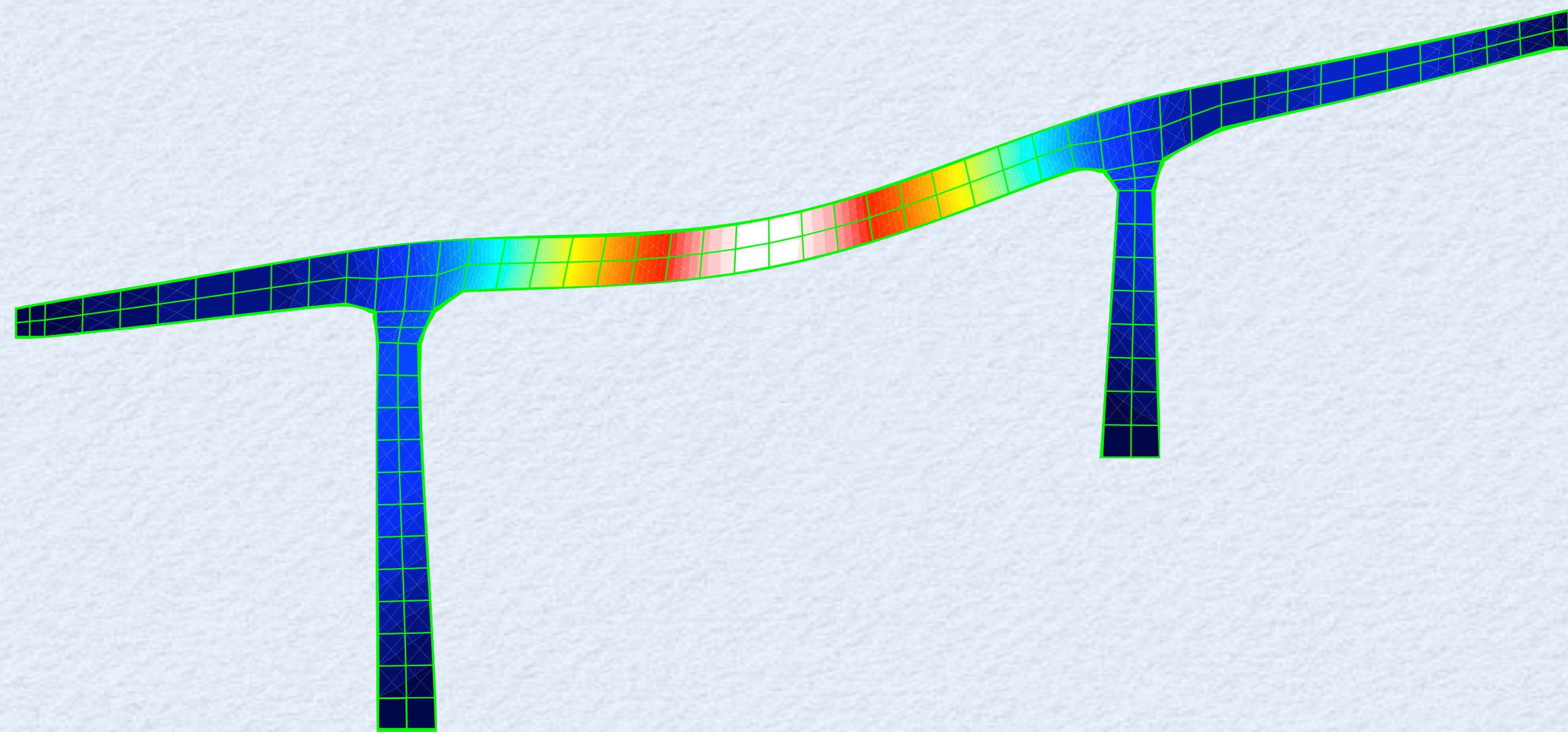
**step 1.** figure out how structures deform





# structural optimization

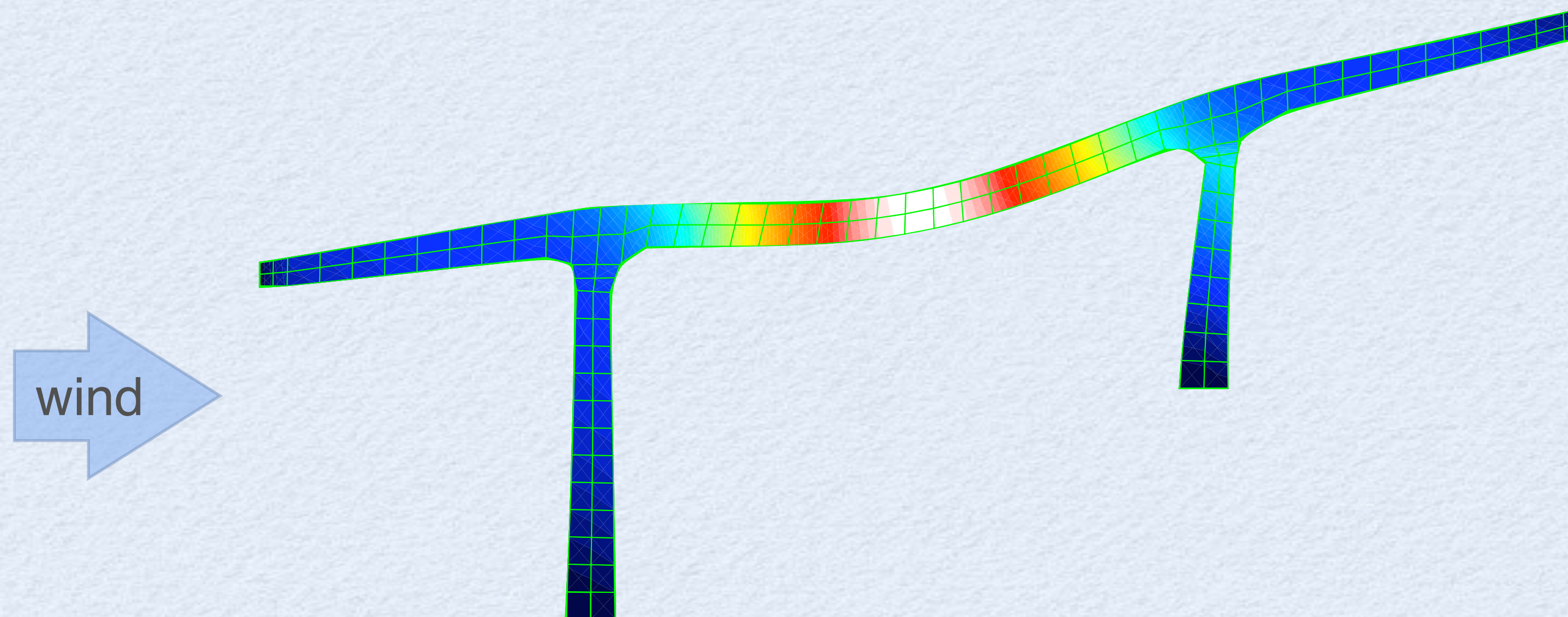
**step 1.** figure out how structures deform





# structural optimization

**step 1.** figure out how structures deform





# structural optimization

**step 1.** figure out how structures deform

linearized elasticity equation

$u$  displacement from initial position

$$u = 0 \quad \text{on} \quad \Gamma_d$$

$$\int_{\Omega} E_{\alpha\beta\gamma\delta}^H e_{\gamma\delta}(u) e_{\alpha\beta}(v) dx = \int_{\Omega} f_{\alpha} v_{\alpha} dx + \int_{\Gamma_t} g_{\alpha} v_{\alpha} dS$$

for all  $v = 0$  on  $\Gamma_d$



# structural optimization

**step 2.** figure out how to measure cost of material

work to build structure

$$k \int_{\Omega} \rho \, dx$$



# structural optimization

step 3. goal

minimize  
 $u, \rho$

$$\int_{\Omega} f_{\alpha} u_{\alpha} dx + \int_{\Gamma_t} g_{\alpha} u_{\alpha} dS + k \int_{\Omega} \rho dx$$

where  $u$  solves

$$u = 0 \quad \text{on} \quad \Gamma_d$$

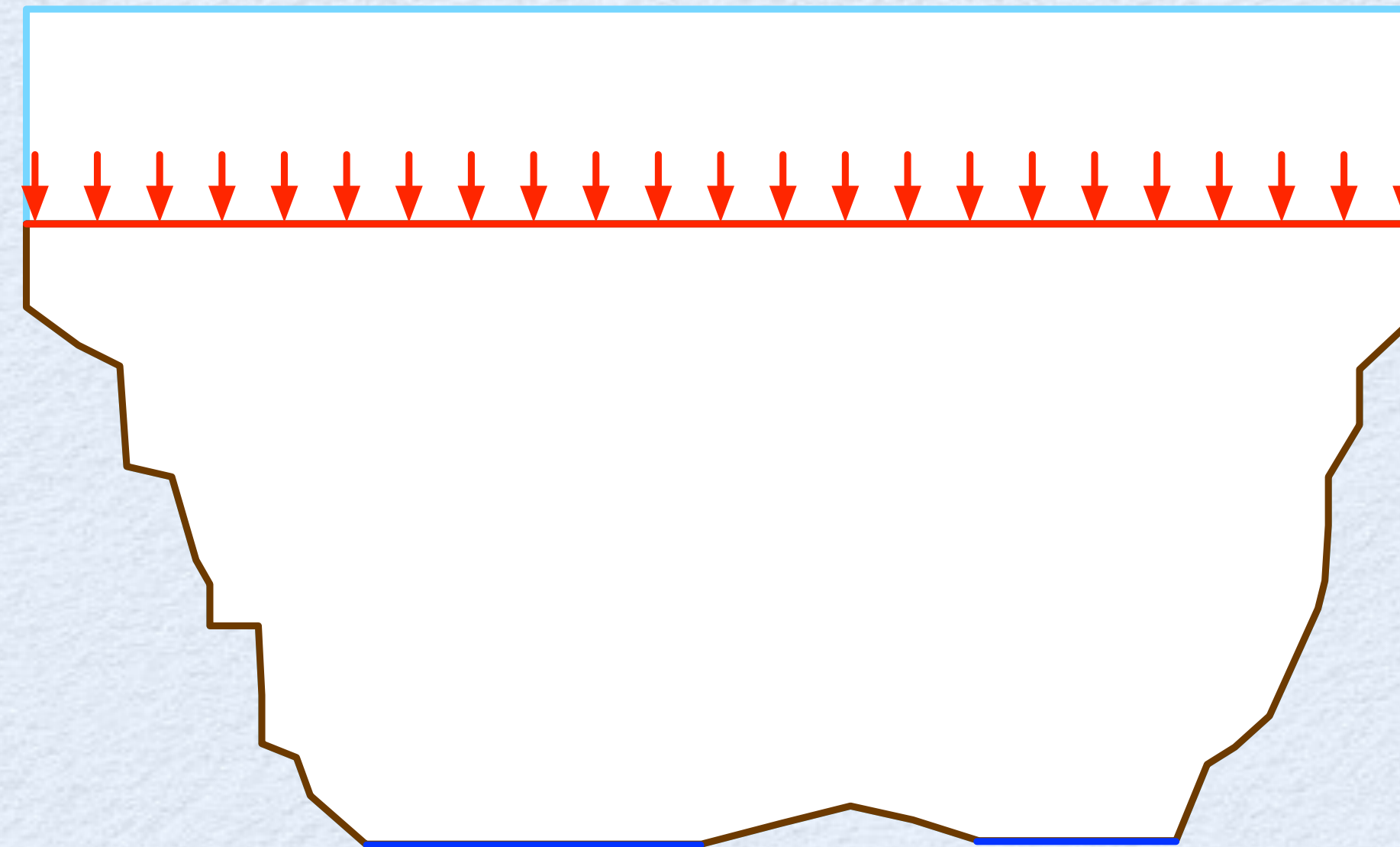
$$\int_{\Omega} E_{\alpha\beta\gamma\delta}(\rho) e_{\gamma\delta}(u) e_{\alpha\beta}(v) dx = \int_{\Omega} f_{\alpha} v_{\alpha} dx + \int_{\Gamma_t} g_{\alpha} v_{\alpha} dS$$

for all  $v = 0$  on  $\Gamma_d$



# structural optimization

step 4. numerical approximation of solution

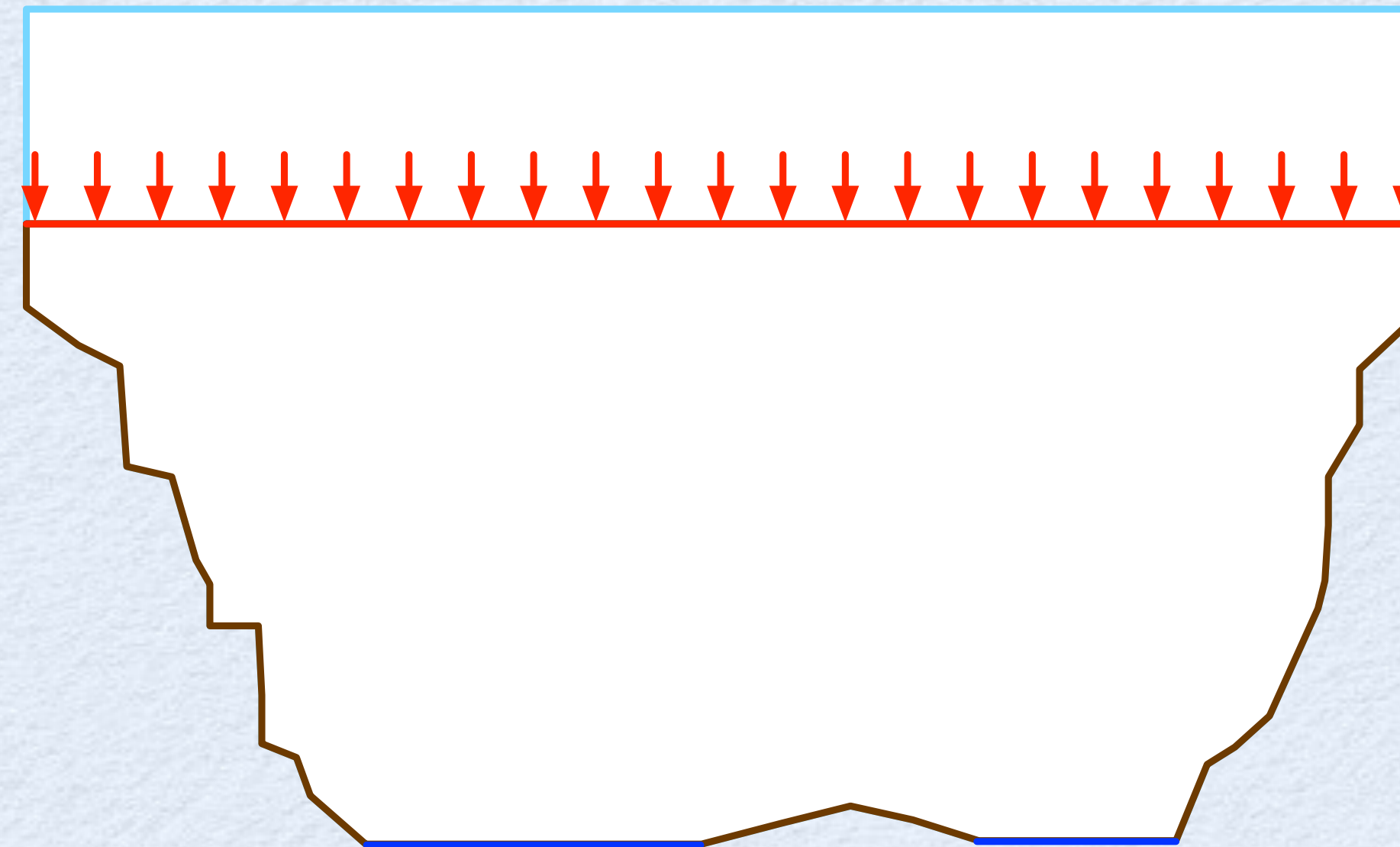




# structural optimization

**step 4.** numerical approximation of solution

**step 4a.** divide the domain in four-sided polygons

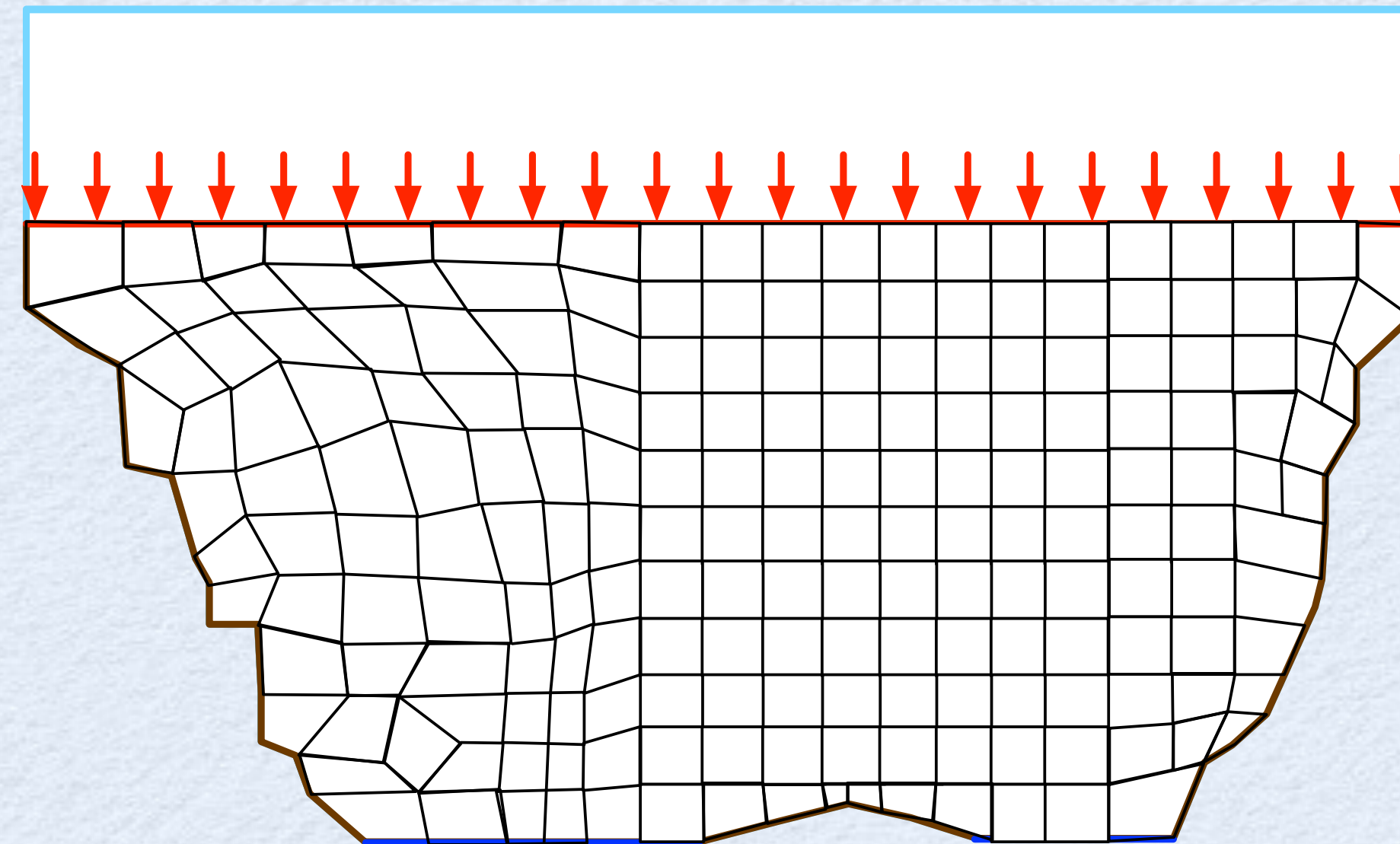




# structural optimization

**step 4.** numerical approximation of solution

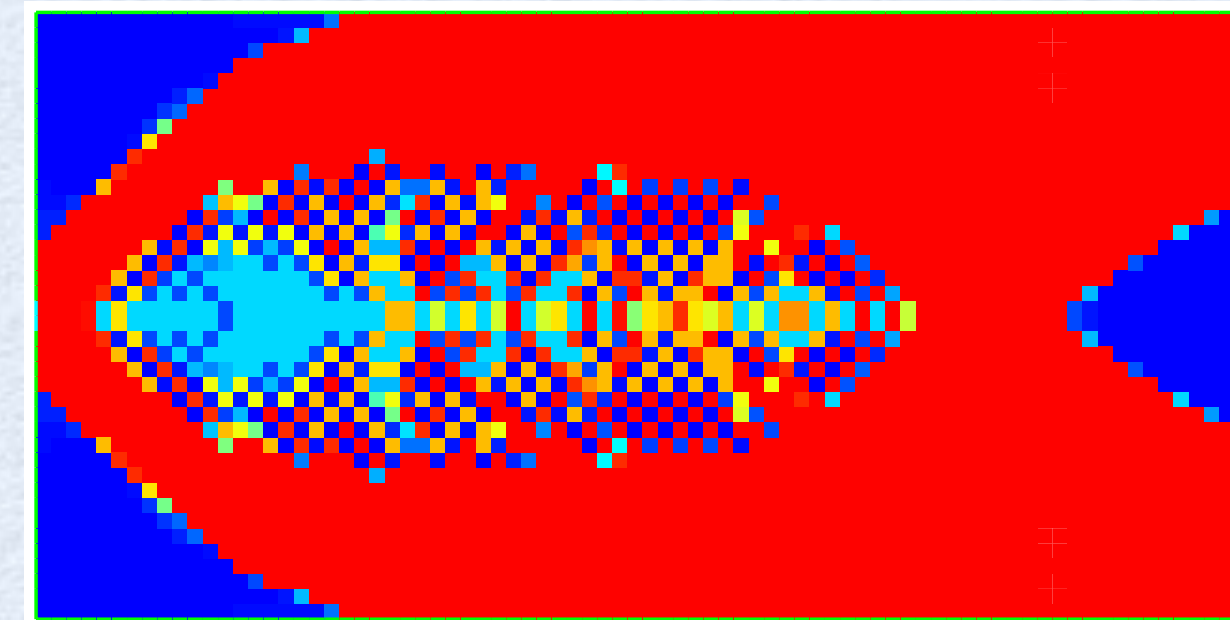
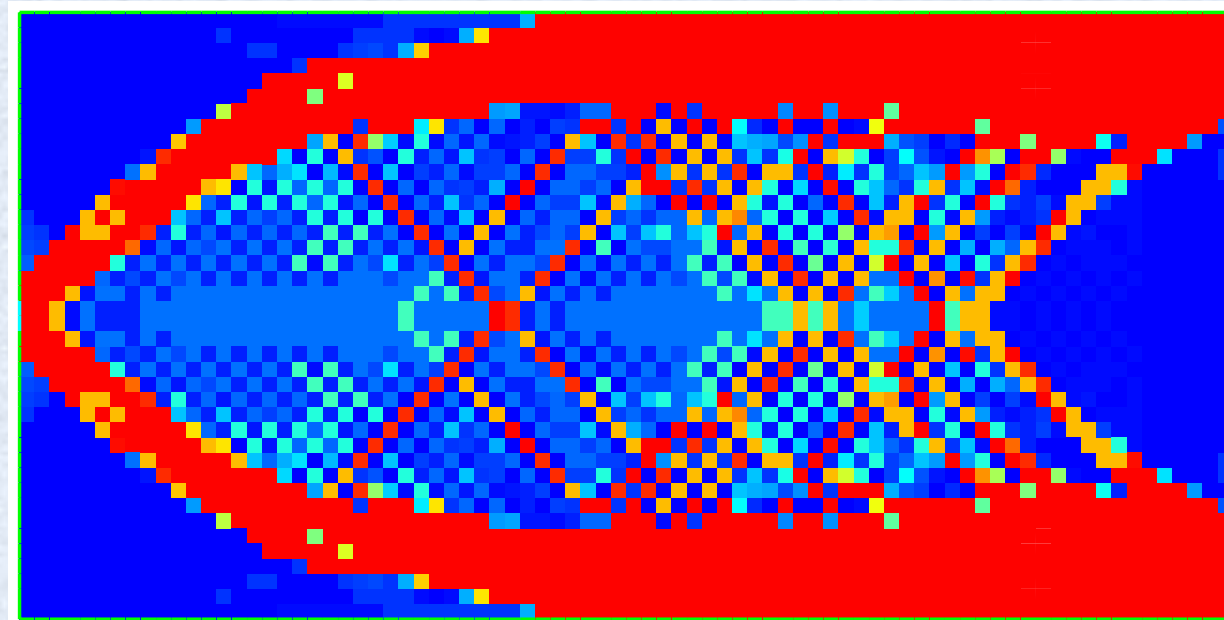
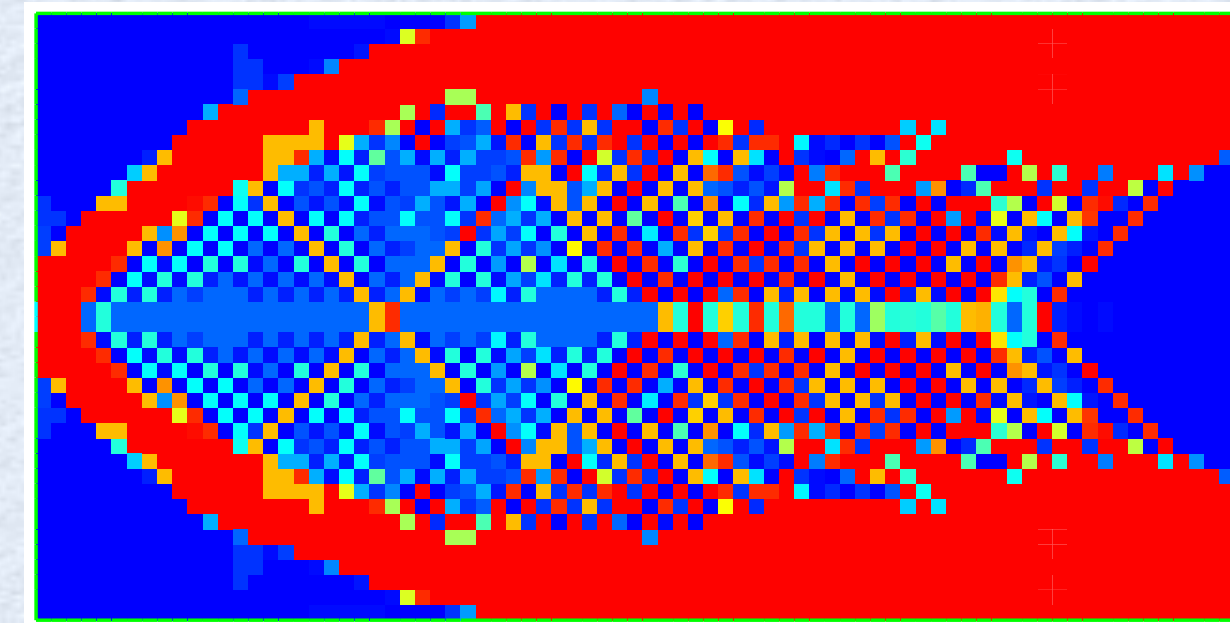
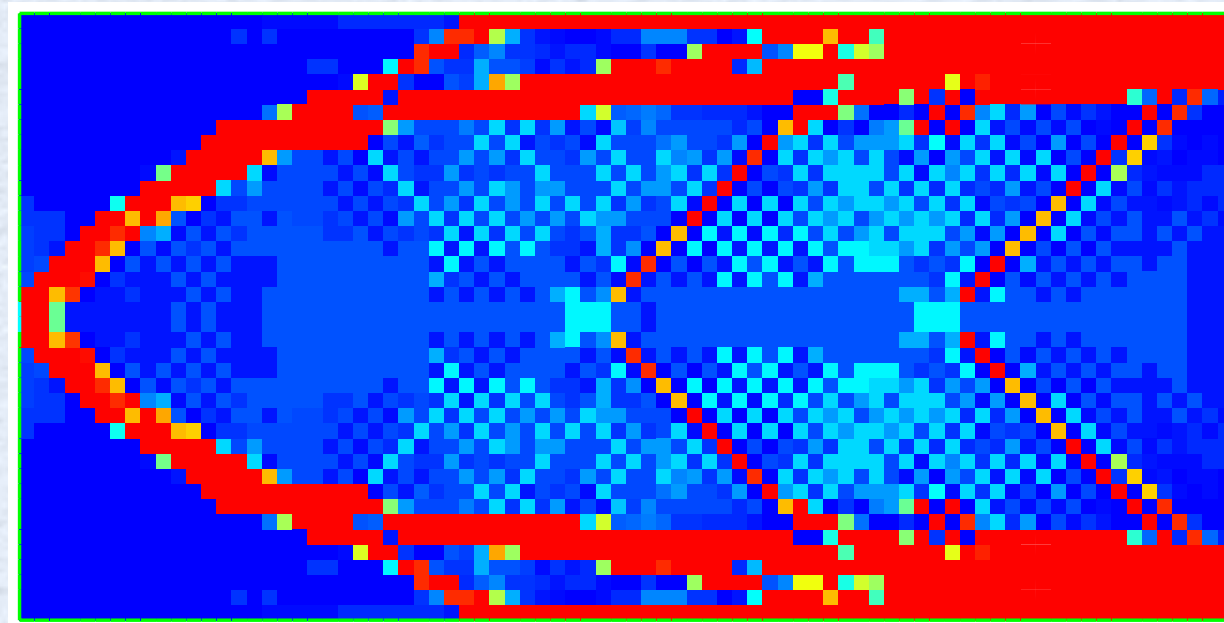
**step 4a.** divide the domain in four-sided polygons





# structural optimization

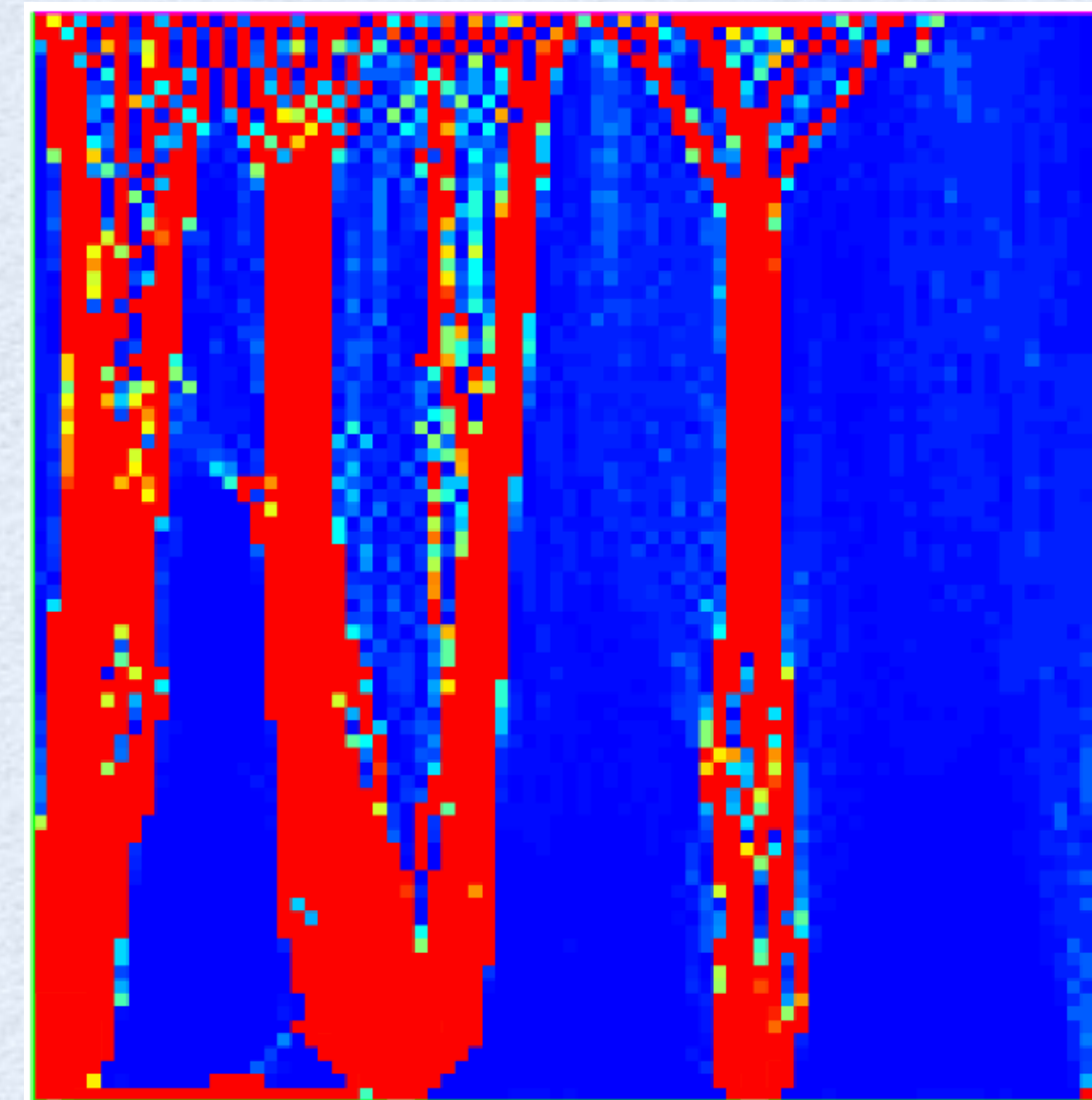
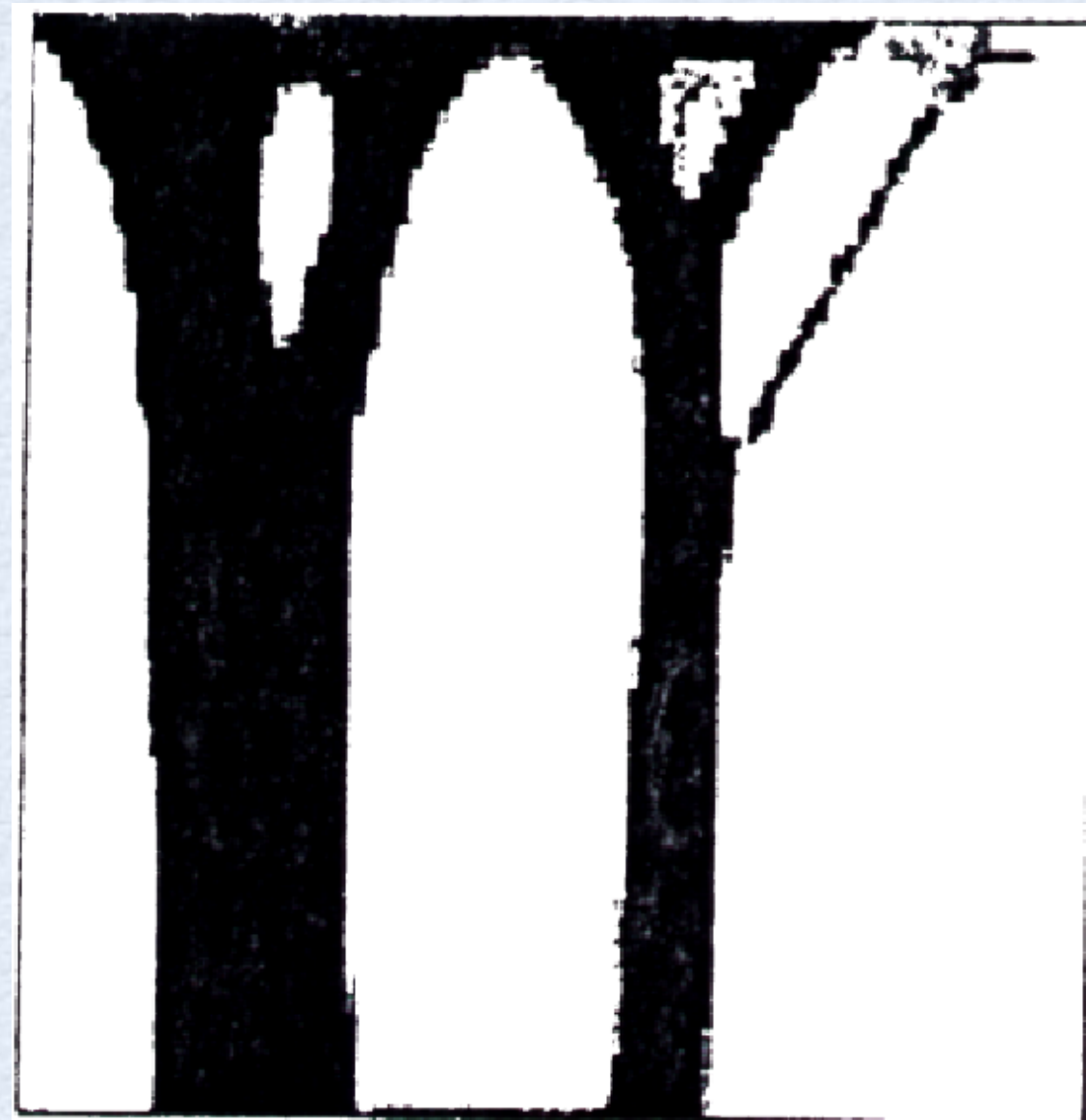
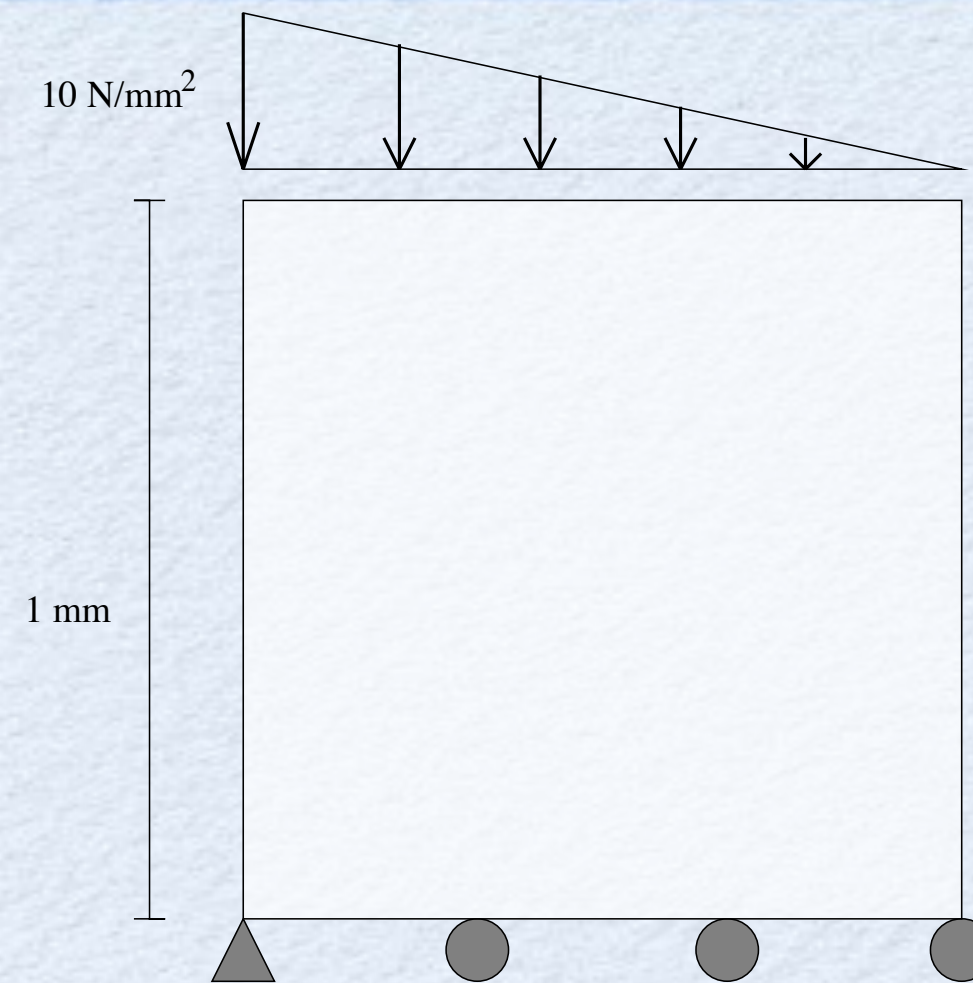
example 1





# structural optimization

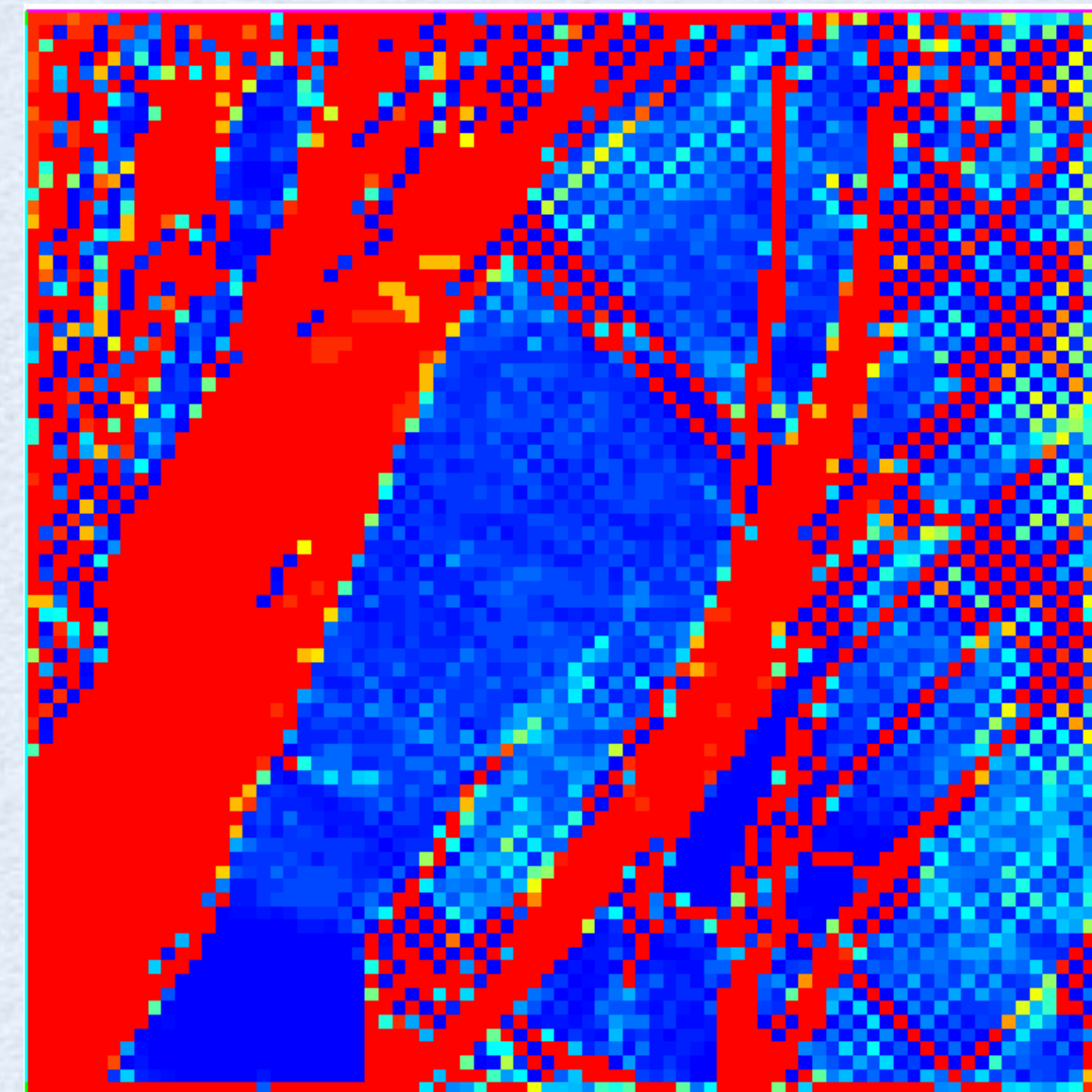
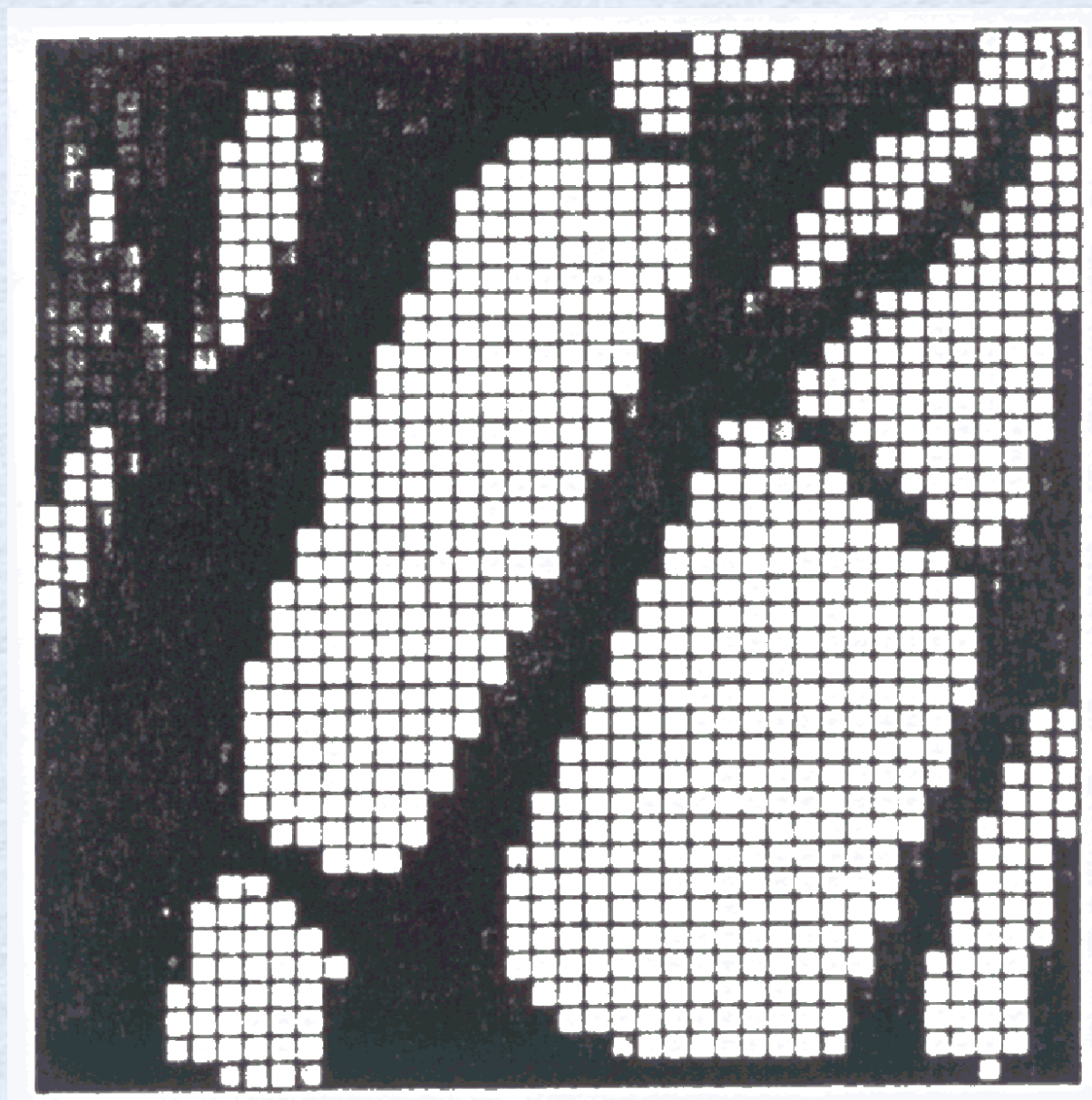
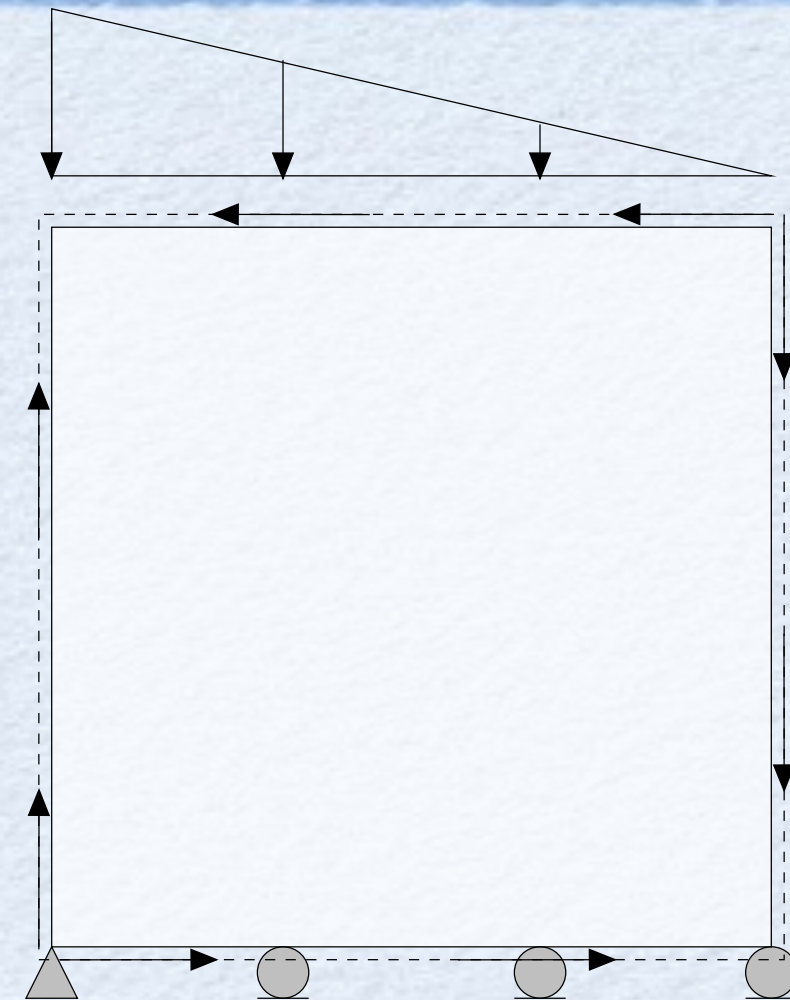
example 2





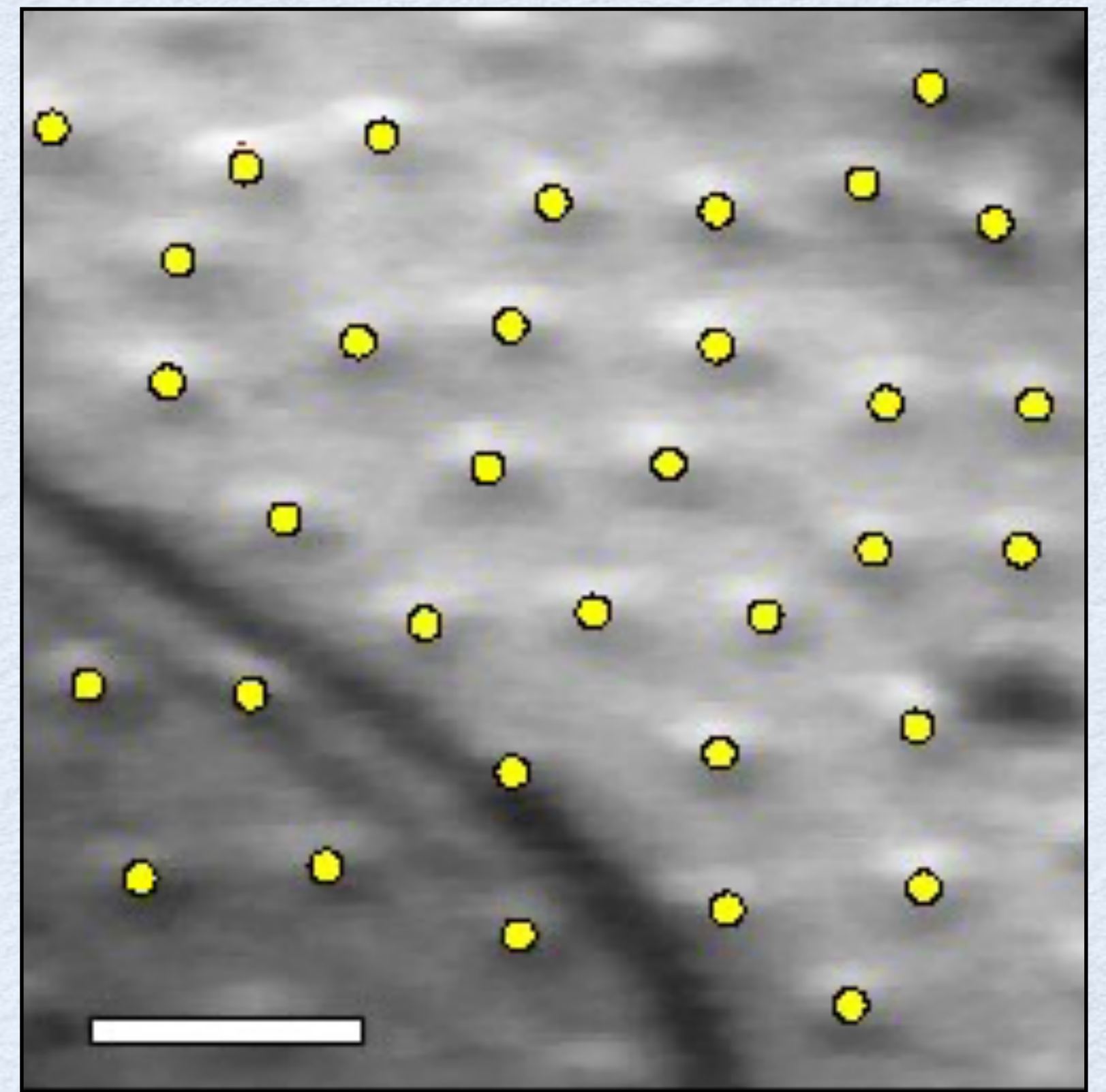
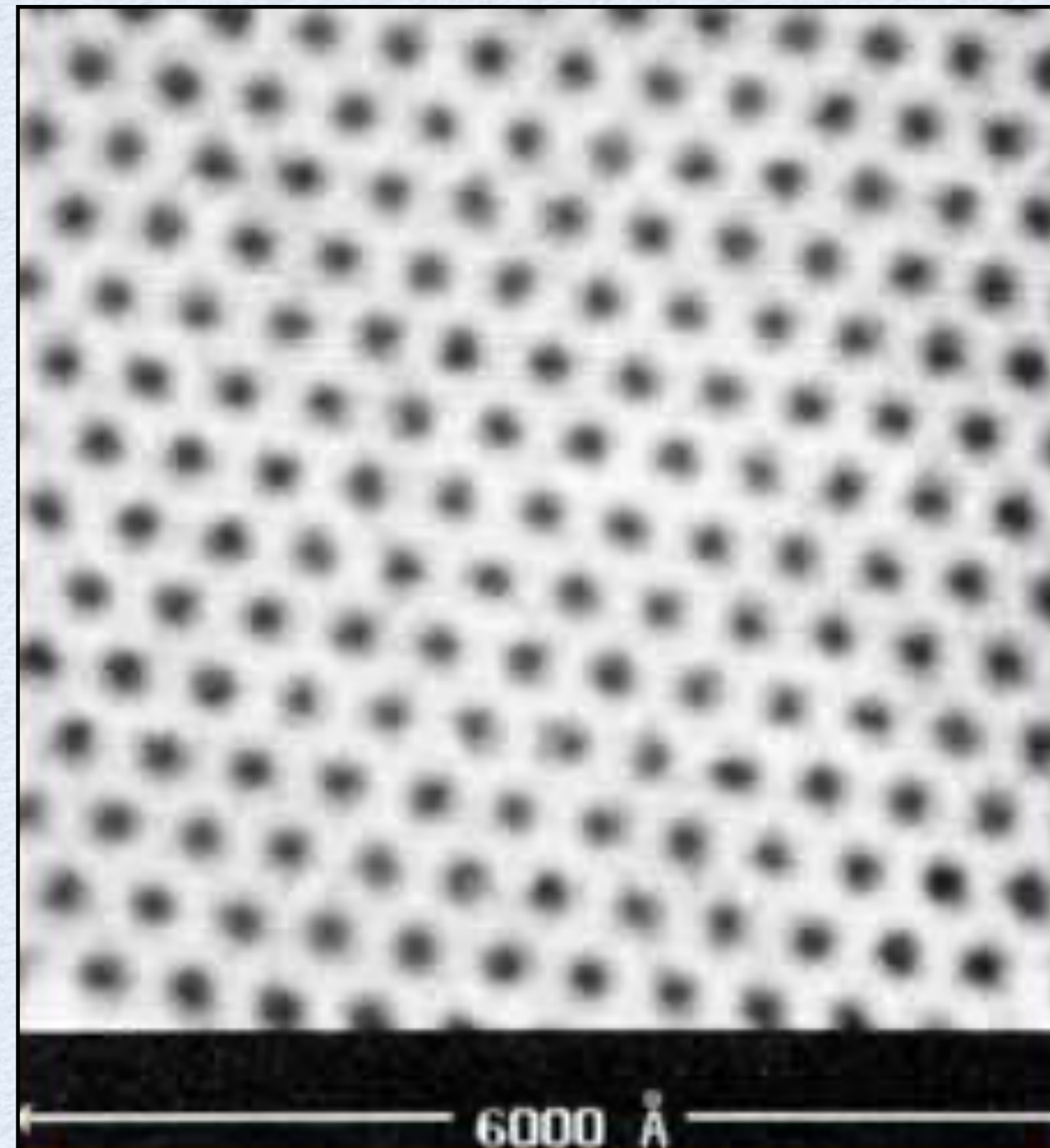
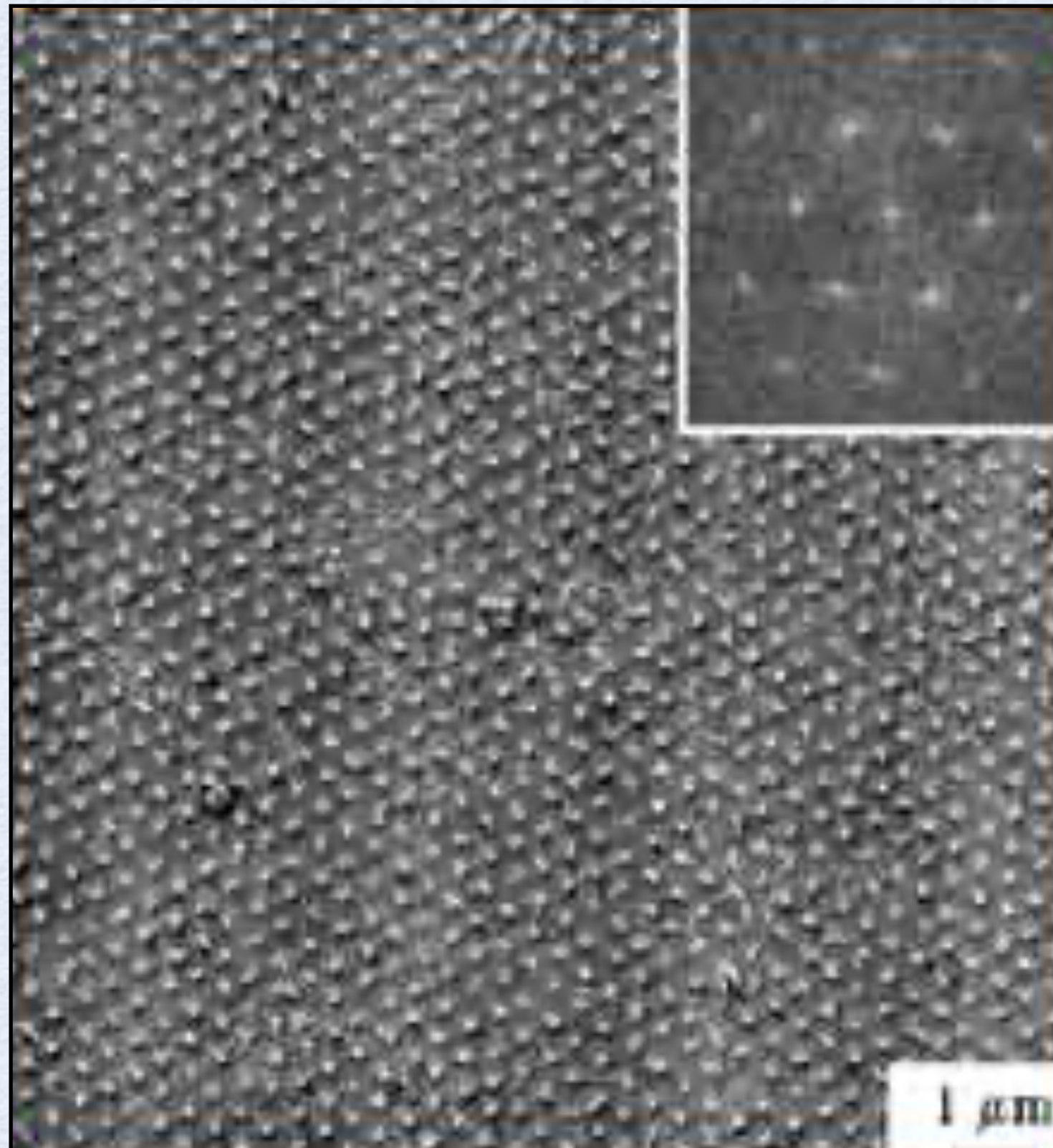
# structural optimization

example 3





# superconducting materials





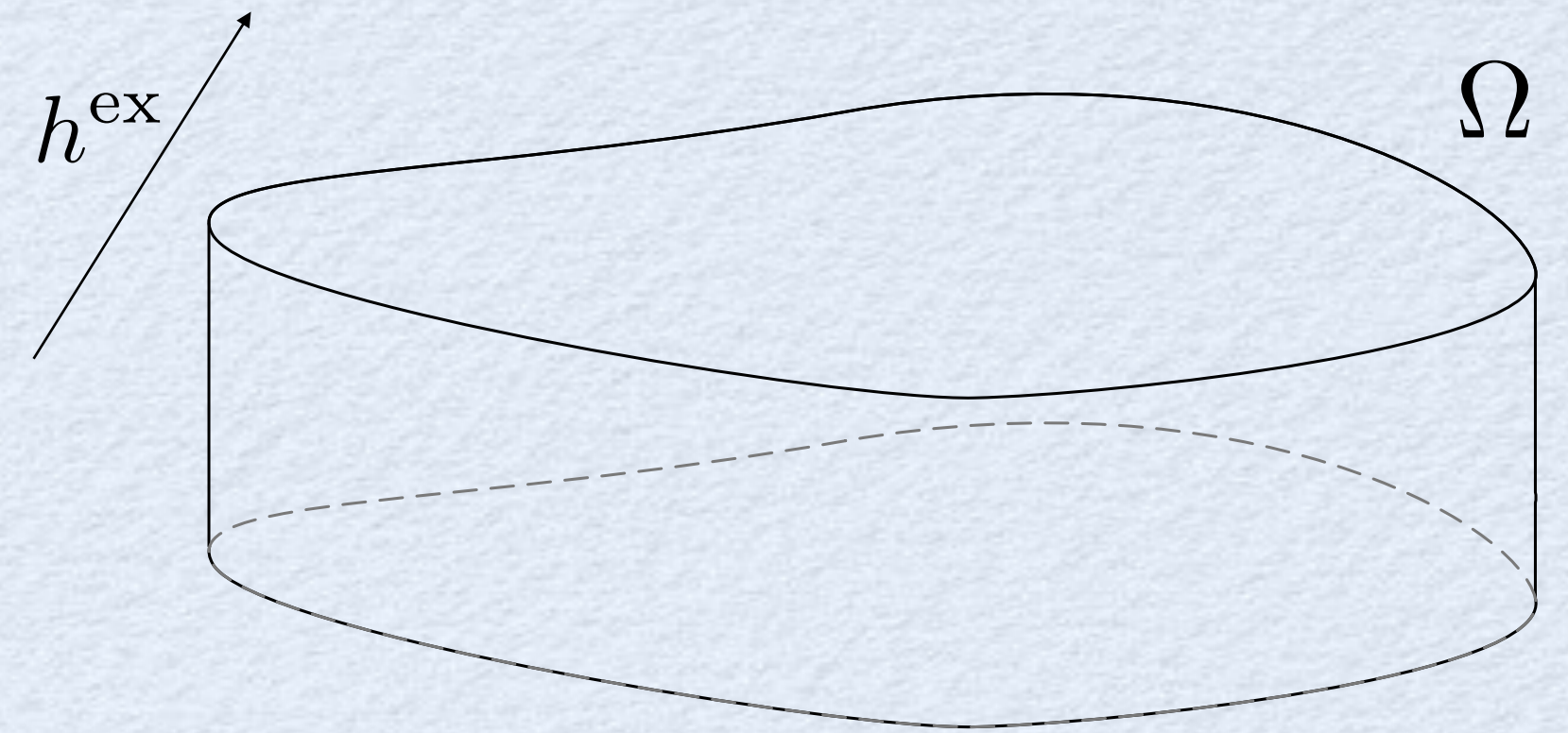
# superconducting materials

$u$  complex order parameter

$A$  electromagnetic vector potential

$h = \nabla \times A$  induced magnetic field

$h^{\text{ex}} = \nabla \times A^{\text{ex}}$  external magnetic field



$$\min_{(u,A)} \left[ \frac{1}{2} \int_{\Omega} \left( |(\nabla - iA)u|^2 + \frac{\kappa^2}{2} (1 - |u|^2)^2 \right) dx + \frac{1}{2} \int_{\mathbb{R}^3} |h - h^{\text{ex}}|^2 dx \right]$$



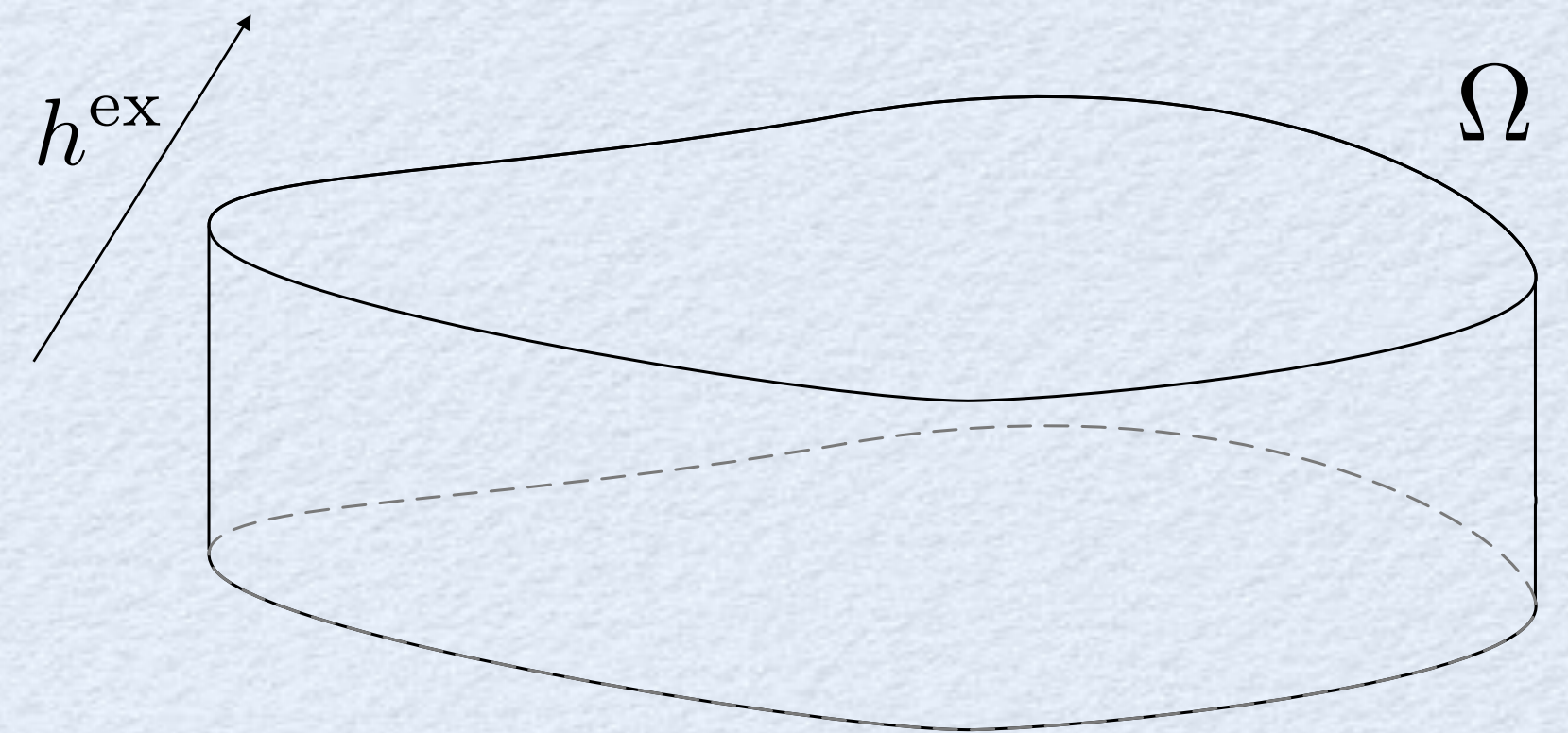
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$$h \approx h^{\text{ex}}$$



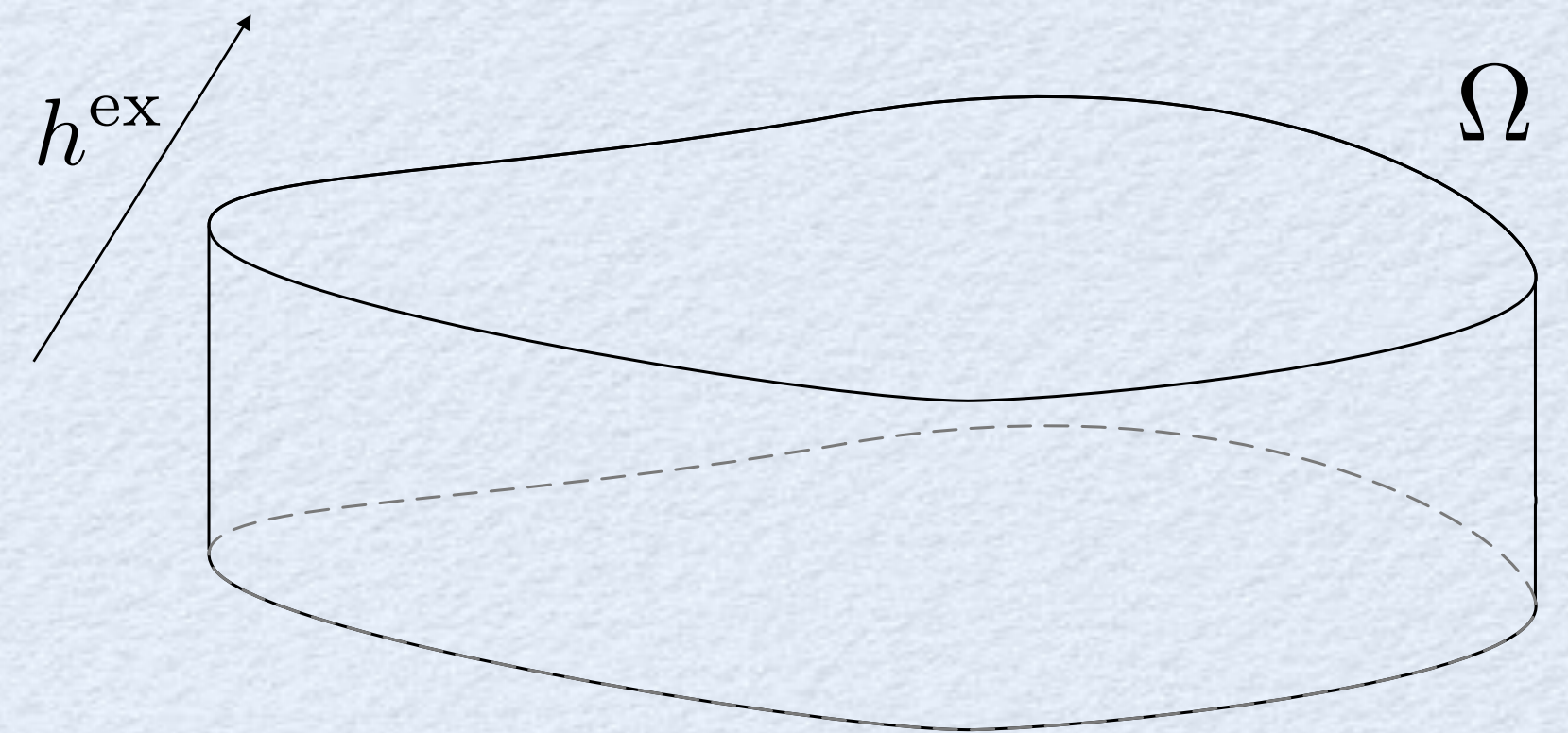
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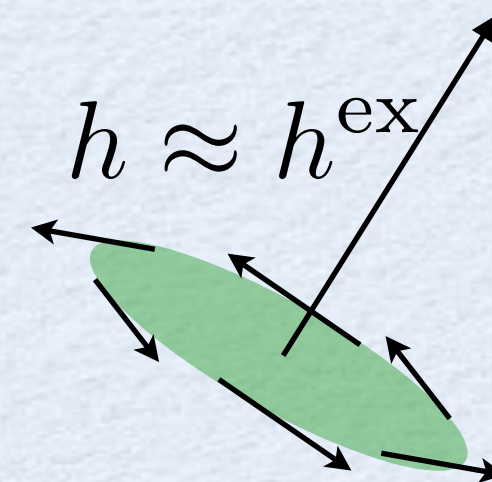
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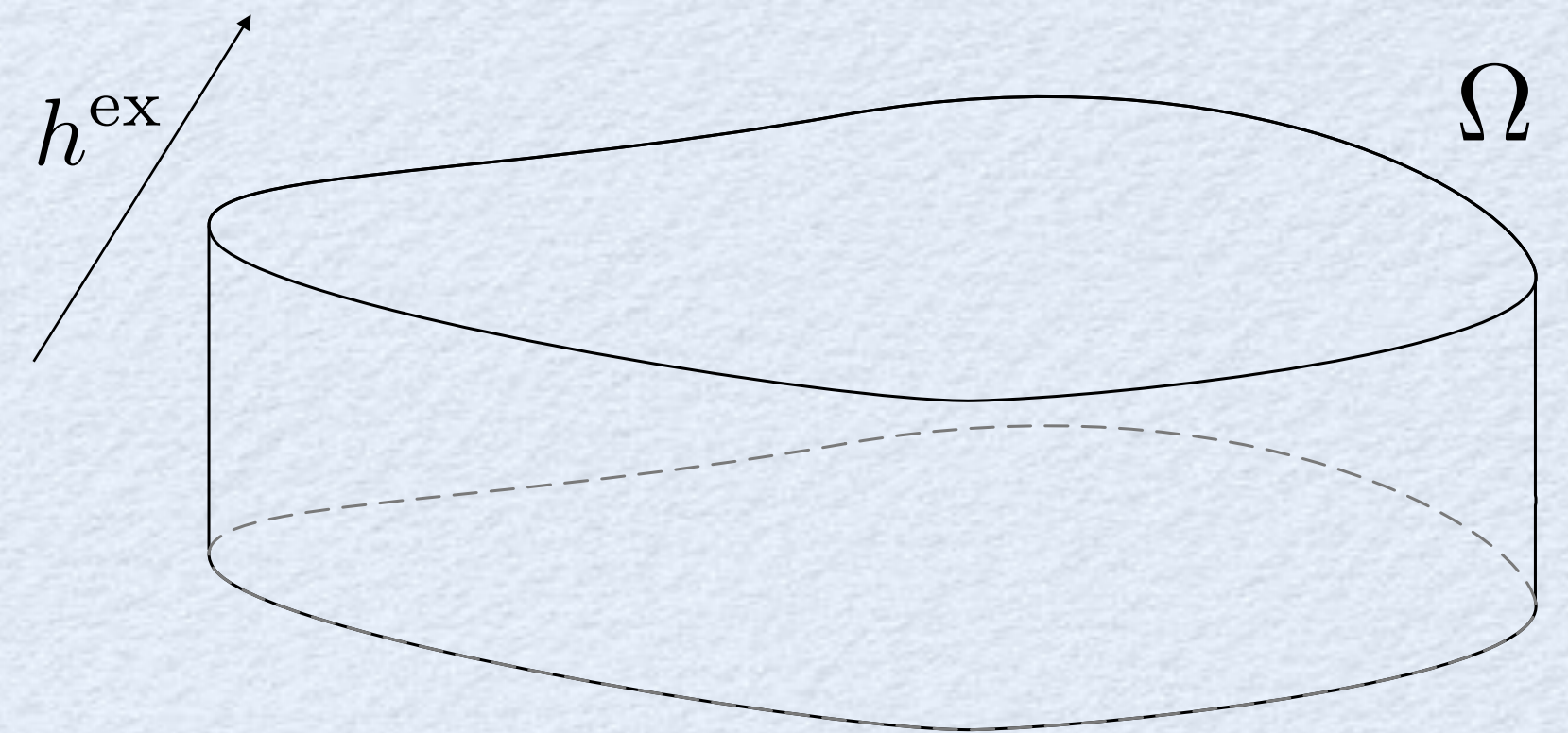
# superconducting materials

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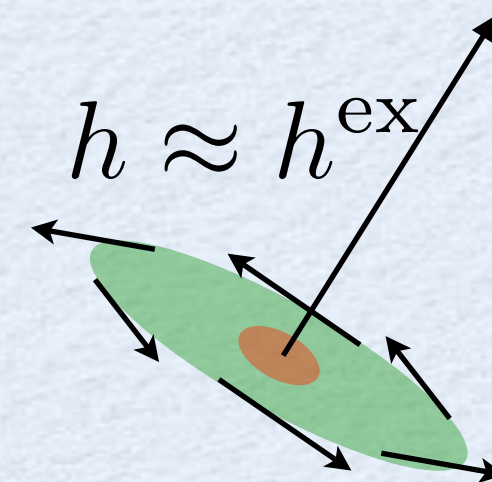
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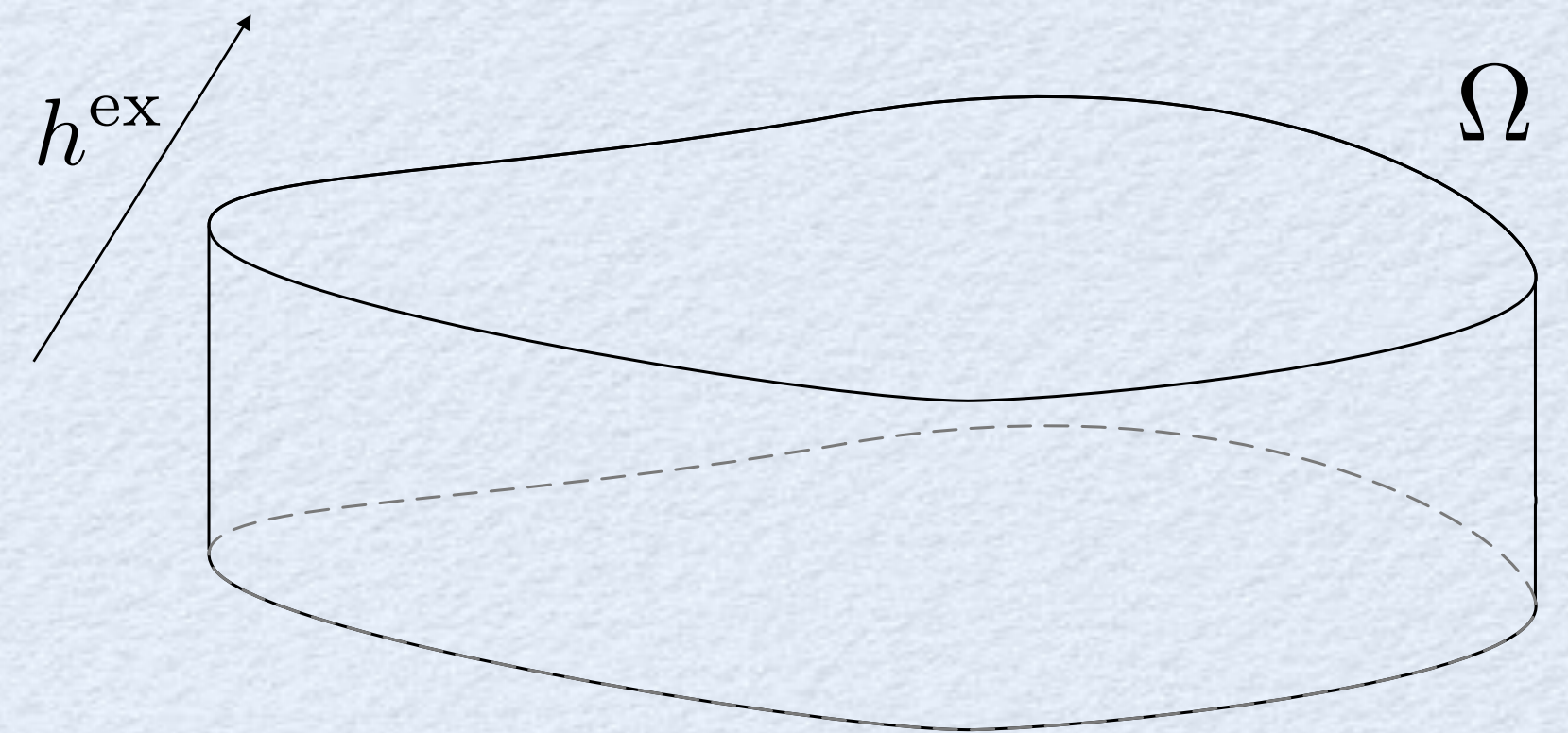
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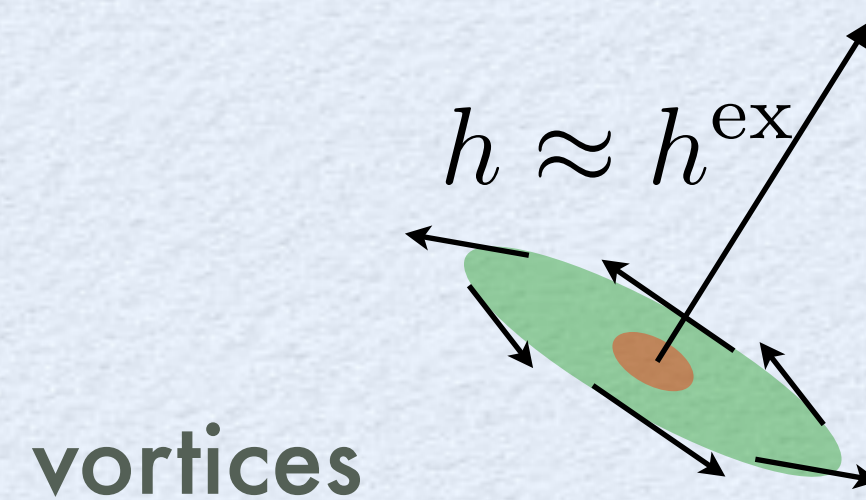
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# superconducting materials





# superconducting materials

