

Apm236h1f 2015
Problems 3

1. Let f, g be two convex functions from \mathbb{R}^n to \mathbb{R} . Let c be a real number. Show that:

(a) $f+g$ is convex.

(b) If $c > 0$, then cf is convex.

2. Convert the following problems to linear programming problems (l.p.p.'s):

(a) minimize $2x + 3|y - 10|$
 subject to $x + y \leq 3$

(b) minimize $\max\{-x, 1, x\}$
 subject to $x \geq 5$

(c) minimize the largest residual (a residual is the prediction error at the i th data point) given the 3 data points $A=(3/4, 1)$, $B=(7/4, 3)$, $C=(11/4, 3)$, and assuming that your function is linear (that is of the form $y=mx$). (At the end, make sure to state your decision variables).

3. Solve the following lpp's.

(a)

Maximize $z = x + y$
 subject to $2x + y \leq 8$
 $x + 3y \leq 9$
 $x \geq 0, y \geq 0$

(b) Same problem as in (a), but Minimize.