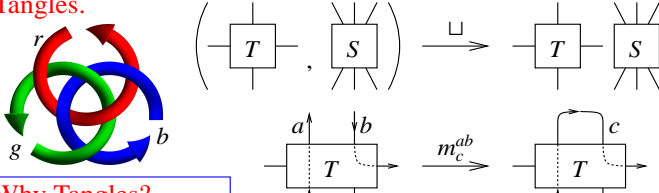


Tangles.



- Finitely presented. (meta-associativity: $m_a^{ab} // m_a^{ac} = m_b^{bc} // m_a^{ab}$)

- $$Z(K) \in \{cl_2(Z): cl_1(Z) = 1\}.$$

$$1. \left(\frac{\omega_1}{S_1} \middle| \frac{S_1}{A_1}, \frac{\omega_2}{S_2} \middle| \frac{S_2}{A_2} \right) \xrightarrow{\sqcup} \frac{\omega_1 \omega_2}{S_1 \mid S_2} \middle| \frac{S_1 \mid S_2}{A_1 \mid A_2} \begin{matrix} 0 \\ 0 \end{matrix},$$

$$2. \quad \begin{array}{c|ccc} \omega & a & b & S \\ \hline a & \alpha & \beta & \theta \\ b & \gamma & \delta & \epsilon \\ S & \phi & \psi & \Xi \end{array} \xrightarrow[\mu:=1-\beta]{m_c^{ab}} \left(\begin{array}{c|cc} \mu\omega & c & S \\ \hline c & \gamma + \alpha\delta/\mu & \epsilon + \delta\theta/\mu \\ S & \phi + \alpha\psi/\mu & \Xi + \psi\theta/\mu \end{array} \right)_{T_a, T_b \rightarrow T_c}$$

and satisfying $(|a\rangle, a \overset{\times}{\prec} b, b \overset{\times}{\prec} a) \xrightarrow{\gamma} \left(\frac{1}{a} |a\rangle, \frac{1}{a} \begin{array}{cc} a & b \\ 1 & 1 - T_a^{\pm 1} \end{array} \right)$.

- $L \mapsto \omega$ is Alexander, mod units.
- $L \mapsto (\omega, A) \mapsto \omega \det'(A - I)/(1 - T')$ is the MVA, mod units.

- 
- A photograph showing two people standing on a series of large, flat, circular stepping stones that cross a pond. The person on the left is wearing a green shirt and khaki pants, and the person on the right is wearing a light blue shirt and dark pants. The pond is surrounded by green foliage and trees.

ωεβ/Demo

$$(\omega, A = (\alpha_{ab})) \leftrightarrow (\omega, \lambda = \sum \alpha_{ab} t_a h_b)$$

```

collect([w_a, a]) := [T*Factor[w],
  collect([h_a, h], collect([T_a, T], Factor[i]);
Format([w_a, a]) := Module[{S, M},
  S = Union[Cases[Factor[w, a], {h[t] t_a -> a, w}],
  M = Order[Factor[Order[Factor[w_a, S], S];
  Prepend[M, {t, w, S}]] & Transpose;
  M = Prepend[M, Prepend[h_a & /@ S, w]];
  M // MatrixForm];

```

$$\text{Meta-Associativity} \quad \gamma = \Gamma \left[\omega, \{t_1, t_2, t_3, t_8\} \cdot \begin{pmatrix} \alpha_{11} & \alpha_{12} & \alpha_{13} & \theta_1 \\ \alpha_{21} & \alpha_{22} & \alpha_{23} & \theta_2 \\ \alpha_{31} & \alpha_{32} & \alpha_{33} & \theta_3 \\ \phi_1 & \phi_2 & \phi_3 & \Xi \end{pmatrix} \cdot \{h_1, h_2, h_3, h_8\} \right]; \quad \text{Runs.}$$



... divide and conquer!

$$\left\{ \begin{array}{ccc|ccc} 1 & h_1 & h_2 & h_3 & 1 & h_1 & h_2 & h_3 \\ t_1 & \frac{T_3}{T_2} & 0 & 0 & t_1 & \frac{T_3}{T_2} & 0 & 0 \\ t_2 & \frac{-1+T_2}{T_2} & \frac{1}{T_3} & 0 & t_2 & \frac{-1+T_2}{T_2} & \frac{1}{T_3} & 0 \\ t_3 & \frac{-1+T_3}{T_2} & \frac{-1+T_3}{T_3} & 1 & t_3 & \frac{-1+T_3}{T_2} & \frac{-1+T_3}{T_3} & 1 \end{array} \right\},$$

```
Do[ $\gamma = \gamma // m_{1k \rightarrow 1}$ , {k, 2, 16}];
```

γ

$$\left(\begin{array}{c} -\frac{1-4T_1+8T_1^2-11T_1^3+8T_1^4-4T_1^5+T_1^6}{T_1^3} \\ t_1 \end{array} \right)$$

h_1

1

\rightarrow

$+15$, $+10$, $+10$, $+10$

-18 , -7 , -9 , -11

8_{17}

- The product ωA is always Laurent, but proving this takes induction with exponentially many conditions.

The diagram shows a central black dot labeled ∞ . Two red circles, labeled u and v , are connected to the central dot by red lines. These circles are labeled "balloons / tails" and are associated with the set T . Two blue circles, labeled x , y , and z , are connected to the central dot by blue lines. These circles are labeled "hoops / heads" and are associated with the set H . A bracket on the left groups the entire structure under the label $\mathcal{K}^{bh}(H; T)$. A bracket on the right indicates that the structure is mapped via "simple embeddings" to \mathbb{R}^4 and S^4 . The text "Simply-knotted balloons and hoops" is written on the left.

Disturbing Conjecture

$\mathcal{K}^{bh} = ?$





Diagram illustrating the Disturbing Conjecture, showing a Feynman diagram with a red line (u) and a blue line (x) interacting at a vertex, and a red line (v) also interacting. The diagram is labeled with $\mathcal{K}^{bh} = ?$.

On the right, a series of diagrams show the reduction of the red line (u) into various topologies labeled R3, R2, VR1, VR2, VR3, M, and OC, with corresponding equations:



- $R3 =$ (diagram)
- $R2 =$ (diagram)
- $VR1 =$ (diagram)
- $VR2 =$ (diagram)
- $VR3 =$ (diagram)
- $M =$ (diagram)
- $OC =$ (diagram)



Dictionary.



“v-xing”



OC:  \leftrightarrow  as  \leftrightarrow 



blue is never “over”



UC:  \leftrightarrow 



UC:  \leftrightarrow 



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

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

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