Cosmic Coincidences and Several Other Stories, 1

Dror Bar-Natan at the University of Tennessee

March 4, 2011, http://www.math.toronto.edu/~drorbn/Talks/Tennessee-1103.

Abstract. In the first half of my talk I will tell a cute and simple story — how given a knot in \mathbb{R}^3 one may count all possible "cosmic coincidences" associated with that knot, and how this count, appropriately packaged, becomes an invariant Z with val-D= ues in some space \mathcal{A} of linear combinations of certain trivalent graphs.

In the second half of my talk I will describe (rather sketchily, I'm The afraid) a part of the story surrounding Z and A: How the same Z also comes from quantum field theory, Feynman diagrams, and configuration space integrals. How \mathcal{A} is a space of universal formulas which make sense in every metrized Lie algebra and The generating function of all cosmic coincidences: how specific choices for that Lie algebra correspond to various famed knot invariants. How Z solves a universal topological problem, and how solving for Z is solving some universal Liealgebraic problem. All together, this is the u-story.

In the remaining time I will mention several other Z's and \mathcal{A}' s and the parallel (yet sometimes interwoven) stories surrounding them — the v-story, and w-story, and perhaps also the p-story Each of these stories is clearly still missing some chapters.

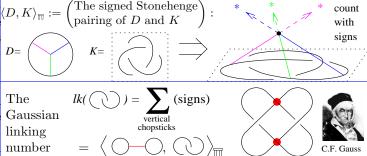
Creation of Adam

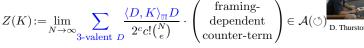


Michelangelo

Disclaimer

We'll concentrate on the beauty and ignore the cracks.





N := # of starsoriented vertices := # of chopsticks :=Span := # of edges of D& more relations

When deforming, catastrophes occur when

A plane moves over an intersection point -Solution: Impose IHX,

(see below)

An intersection line cuts through the knot -Solution: Impose STU,

(similar argument)

The Gauss curve slides Solution: Multiply by a framing-dependent counter-term. (not shown here)

Theorem. Modulo Relations, Z(K) is a knot invariant!

