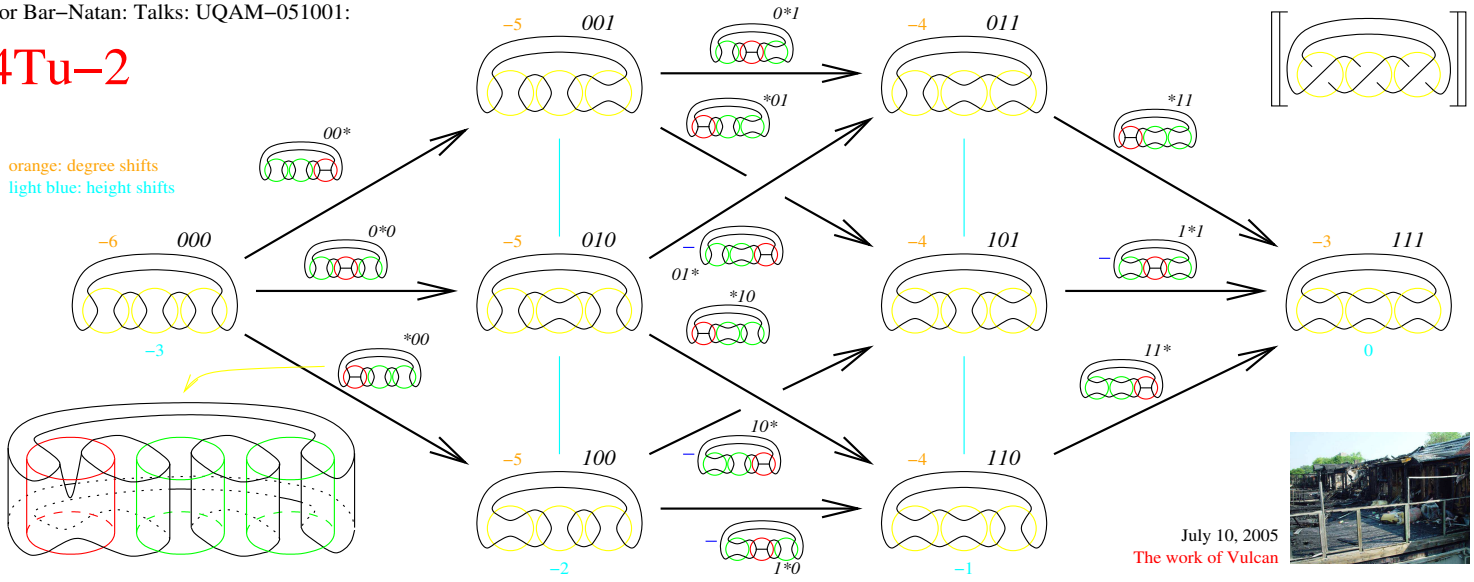
Dror Bar–Natan: Talks: UQAM–051001:

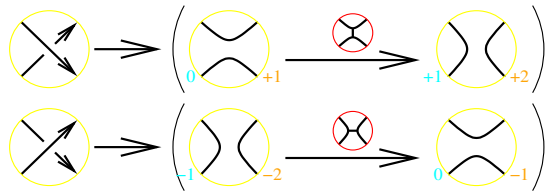
4Tu–2

orange: degree shifts
light blue: height shifts



July 10, 2005
The work of Vulcan

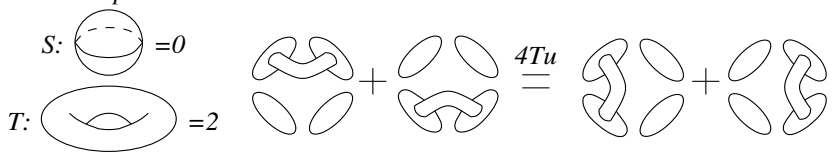
General Crossings



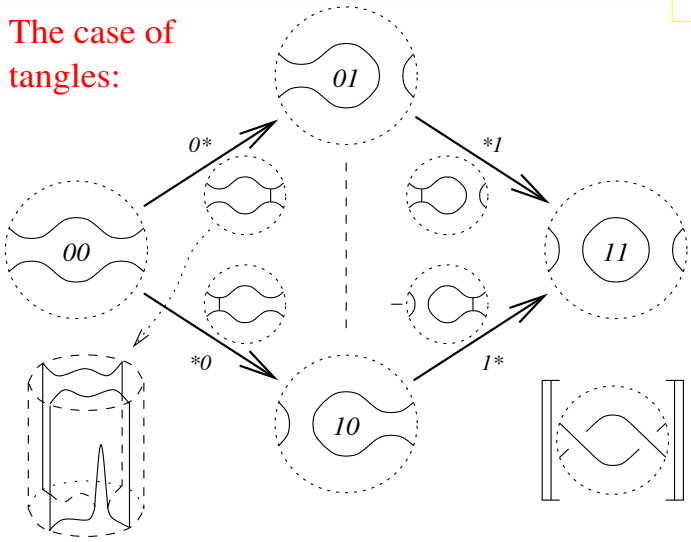
Where does it live?

In *Kom(Mat(<Cob> / {S, T, 4Tu})) / homotopy*

Kom: Complexes Mat: Matrices Cob: Cobordisms <...>: Formal lin. comb.

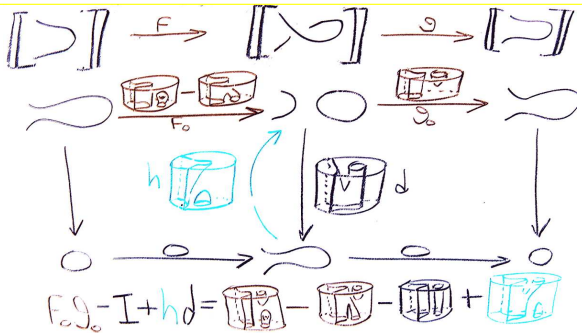


The case of tangles:



Invariant!

Kurt Reidemeister



The Reduction Lemma. If ϕ is an isomorphism then the complex

$$[C] \xrightarrow{\begin{pmatrix}\alpha\\ \beta\end{pmatrix}} \begin{bmatrix} b_1 \\ D \end{bmatrix} \xrightarrow{\begin{pmatrix}\phi & \delta\\ \gamma & \epsilon\end{pmatrix}} \begin{bmatrix} b_2 \\ E \end{bmatrix} \xrightarrow{\begin{pmatrix}\mu & \nu\end{pmatrix}} [F]$$

is isomorphic to the (direct sum) complex

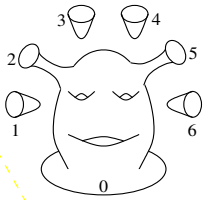
$$[C] \xrightarrow{\begin{pmatrix}0\\ \beta\end{pmatrix}} \begin{bmatrix} b_1 \\ D \end{bmatrix} \xrightarrow{\begin{pmatrix}\phi & 0\\ 0 & \epsilon-\gamma\phi^{-1}\delta\end{pmatrix}} \begin{bmatrix} b_2 \\ E \end{bmatrix} \xrightarrow{\begin{pmatrix}0 & \nu\end{pmatrix}} [F]$$

The work of Naot.

<surfaces>/4Tu is freely generated by Shrek surfaces

Gad Naot

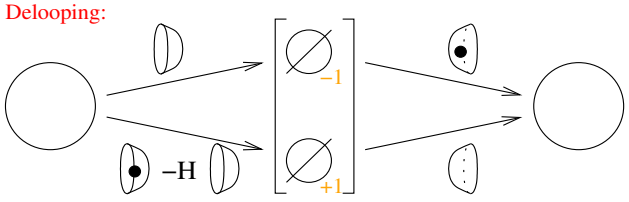
A Shrek surface with 7 boundaries (one distinguished), 3 handles and 2 tubes



שרעק

Let ● denote a tube to the distinguished component (the curtain), and let H denote a handle on the curtain. Then

Delooping:

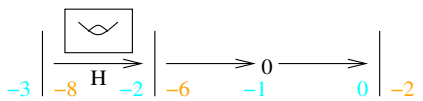


... so the invariant is valued in complexes over a category with just one object and morphisms in Z[H]; all is graded and degH=−2.

The work of Green.

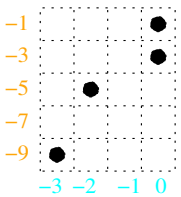
Jeremy Green

The universal invariant of the left–handed trefoil is

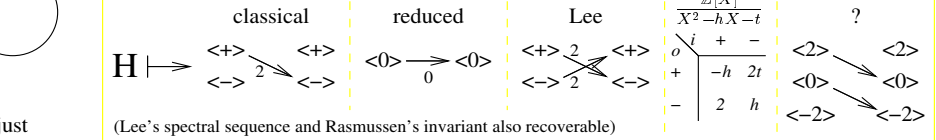


(and the invariant of the 48 crossing T(8,7) is computable in minutes...)

standard data:



Some functors.



(Lee's spectral sequence and Rasmussen's invariant also recoverable)

http://www.math.toronto.edu/~drorbn/Talks/UQAM–051001/

More at http://www.math.toronto.edu/~drorbn/Talks/UQAM-051001/