

- (1) Show that interior of any set is an open set.
- (2) finish the proof of the following statement from class. For any set $A \subset R^n$ we have

$$R^n = \text{int}(A) \cup \text{ext}(A) \cup \partial(A)$$

and none of the three sets $\text{int}(A), \text{ext}(A), \partial(A)$ intersect.

- (3) show that

$$\left(\sum_{i=1}^n x_i y_i\right)^2 \leq \left(\sum_{i=1}^n x_i^2\right) \left(\sum_{i=1}^n y_i^2\right)$$

using the same method as was used in class to prove it for $n=2$.

- (4) Show that a set $A \subset R^n$ is closed if and only if it contains all its boundary points.
- (5) construct a closed Cantor set $A \subset [0, 1]$ of positive measure.

Extra Credit Problem (to be written up and submitted separately)

Suppose v_1, \dots, v_{k+1} are nonzero vectors in R^n such that $\angle v_i v_j > \pi/2$ for any $i \neq j$.

Show that v_1, \dots, v_k are linearly independent.