- (1) Finish the proof of the theorem from class: If  $f: A \to R^m$  is continuous where  $a \subset R^n$ , then for any open set  $U \subset R^m$ , there is an open set  $V \subset R^n$  such the  $f^{-1}(U) = V \cap A$ .
- (2) Finish the proof of theorem from class: Let  $f: \mathbb{R}^n \to \mathbb{R}^m$  satisfies the following property.

For any sequence  $x_k \to p$  we have  $f(x_k) \to f(p)$ .

Then f is continuous at p.

*Hint:* Assume that f is not continuous at p and construct a sequence  $x_k \to p$  such that  $f(x_k) \not\to f(p)$ .

## Extra Credit Problem (to be written up and submitted separately)

Let  $A = \{x \in \mathbb{R}^n | \text{such that } 1 \leq |x| \leq 2\}$  and  $f \colon A \to \mathbb{R}$  be a continuous function. Let  $M = \sup_{a \in A} f(a)$  and  $m = \inf_{a \in A} f(a)$ . prove that F(A) = [m, M].