

**HOMEWORK SET #2: DUE SEPTEMBER 30**

- (1) Munkres:
- §16 2
  - §17 13,19
  - §18 6, 13
  - §19 8
  - §20 6, 8
- (2) Suppose  $Y$  is a topological space,  $X$  is a set and  $f : X \rightarrow Y$  is a function. Prove that there is a coarsest topology on  $X$  for which  $f$  is continuous.
- (3) let  $I$  be an uncountable set, and let  $X = \prod_{i \in I} \mathbb{R}$ . Each  $\mathbb{R}$  is equipped with the standard topology, and  $X$  is equipped with the corresponding product topology. Prove that  $X$  is not metrizable. What about if  $X$  is equipped with the corresponding box topology?